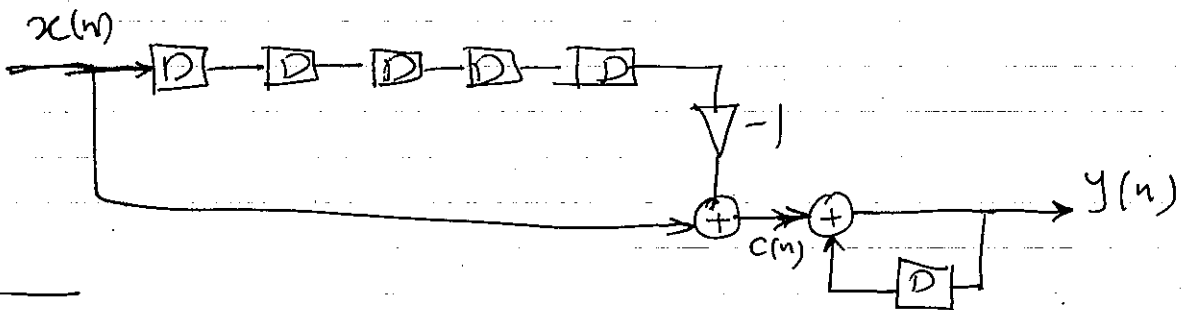
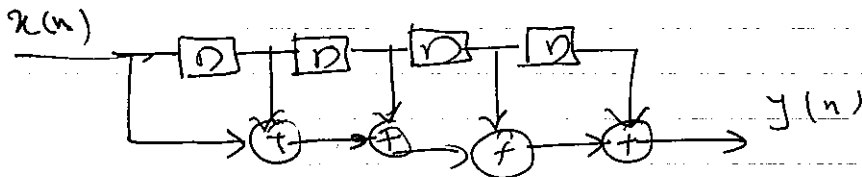


10/2

Show that both of the following circuits are equal (having the same difference equation).



for first one, we have:

$$y(n) = x(n) + x(n-1) + x(n-2) + x(n-3) + x(n-4)$$

$$= \sum_{k=0}^4 x(n-k)$$

for second:

$$\begin{cases} c(n) = x(n) - x(n-5) \\ y(n) = c(n) + y(n-1) \\ y(n-1) = c(n-1) + y(n-2) \\ y(n-2) = c(n-2) + y(n-3) \\ y(n-3) = c(n-3) + y(n-4) \\ y(n-4) = c(n-4) + y(n-5) \\ y(-1) = 0 \end{cases}$$

$$y(n) = \sum_{i=0}^n c(i)$$

$$y(n) = \sum_{i=0}^n x(i) - x(i-5)$$

$$= x(n) + x(n-1) + x(n-2) + x(n-3) + x(n-4) + x(n-5) + \dots + x(1) + x(0) - [x(n-5) + \dots + x(1) + x(0)]$$

$$= \sum_{k=0}^4 x(n-k)$$

Then two circuits are equal.