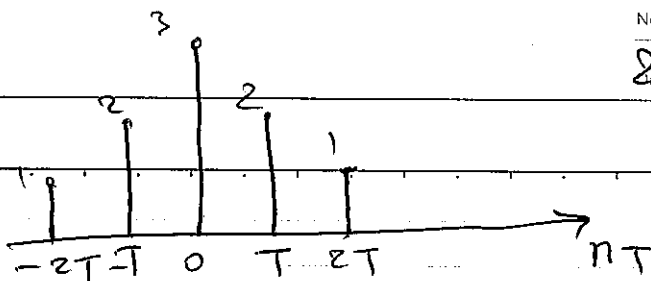


3.6



$$X(\omega) = \sum_{n=-\infty}^{+\infty} x(nT) e^{-j\omega nT}$$

$$X(\omega) = e^{j2\omega T} + 2e^{j\omega T} + 3 + 2e^{-j\omega T} + e^{-j2\omega T}$$

$$X(\omega) = (e^{j\omega T} + 1 + e^{-j\omega T})^2$$

Since:

$$S = 1 + q + q^2 + \dots + q^n$$

$$- [qS = q + q^2 + q^3 + \dots + q^n + q^{n+1}]$$

$$(1-q)S = 1 - q^{n+1} \rightarrow S = \frac{1 - q^{n+1}}{1 - q}$$

If:

$$S = e^{j\omega T} + 1 + e^{-j\omega T}$$

$$- [e^{j\omega T} S = e^{j\omega T} + e^{j2\omega T} + e^{j3\omega T} + \dots]$$

$$S(1 - e^{j\omega T}) = e^{-j\omega T} - e^{j2\omega T}$$

$$S = \frac{e^{-j\omega T} - e^{j2\omega T}}{1 - e^{j\omega T}} = \frac{e^{-\frac{j\omega T}{2}} (e^{-\frac{j3\omega T}{2}} - e^{\frac{j3\omega T}{2}})}{e^{-\frac{j\omega T}{2}} (e^{-\frac{j\omega T}{2}} - e^{\frac{j\omega T}{2}})}$$

$$S = \frac{\sin \frac{3\omega T}{2}}{\sin \frac{\omega T}{2}}$$

$$X(\omega) = S^2 = \left(\frac{\sin \frac{3\omega T}{2}}{\sin \frac{\omega T}{2}} \right)^2$$