

Simulation
3-rd year undergraduate
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Time: 90 minutes (write answers in boxes)

Use the table-look-up method to simulate random variables X from U(0,1).

Where the p.d.f of X is: $f(x)=2x/(1+x^2)$, $0 \leq x < (e-1)^{1/2}$ 10%
(Hint: see page 95)

Simulate the random variable X with the following probabilities:

(Hint: see page 93)

From a U(0,1) in the following table:

10%

- 3- The mixed congruential generator: $EMBED \text{ Equation.3} \pmod{8}$ has full 8 cycle-length. With seed $EMBED \text{ Equation.3}$, simulate all cycles, one after each.

15%

(Hint: See page 61)

- 4- Simulate the normal distributed random variables (N1, N2) by using The Box-Muller method from the following U1, U2 uniform distributed random variables: U1=0.4, U2=0.6 15%

(Hint: See page 78 Eq. 4.1)

- 5- Simulate a Binomial random variable X with B(8,0.75) from a set of uniform random variables U (0,1), by using Bernouli random variable, where:

U1=0.8, U2=0.2, U3=0.7, U4=0.5, U5=0.9, U6=0.6, U7=0.3, U8=0.4 10%

(Hint: See page 82)

p=0.75

- 6-Simulate random variable X with geometric distribution and p=0.5 from U(0,1)=0.2

(Hint: See page 93 Eq. 5.4)

10%

7- Simulate a Poisson distribution random variable, K , with parameter $\lambda=1$ from the following uniform random variables: $U=\{0.7, 0.8, 0.9, 0.5\}$

(Hint: See page 84)

10%

8- In randomized response technique (RRT), if we have $P0=0.4$, and $\Pr[N | \text{Yes}]=0.8$, and total probability from survey is: $\Pr[\text{Yes}]=0.9$, find the $\Pr[E | \text{Yes}] = ?$

(Hint: See page 51)

10%

I	0	1	2	3	4	5	6
$\Pr[X < I]$	0.15	0.24	0.37	0.58	0.75	0.95	0.99

$X =$

$\Pr[E | \text{Yes}] =$

$x(0)=1, x(1)=, x(2)=, x(3)=, x(4)=, x(5)=, x(6)=, x(7)=$

$(N1=, N2=$

$X =$

$X =$

U 0.94 0.85 0.16 0.68 0.35 0.56 0.97

X

K =