| Simulation Exam(B) Name: | University of the Ryukyus |
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| 3-rd year undergraduate No: | Faculty of Engineering |
| 2004-2-16 | Department of Information Eng. |
| Time: 90 minutes (write answers in boxes) | Prof. M.R. Asharif |
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1- In the mixed congruential generator: EMBED Equation. 3 simulate the first seven numbers with seed EMBED Equation. 3 . Then find the correlation between two successive numbers.

$$
5 \%
$$

$10 \%$
(Hint: See page 60-61)
2- Simulate the normal distributed random variables (N1, N2) by using Polar-Marsaglia method (rejection method) from each pair of the following uniform distributed random variables: (Hint: See page 80)

$$
(\mathrm{V} 1, \mathrm{~V} 2)=(0.4,0.6),(\mathrm{V} 1, \mathrm{~V} 2)=(0.5,0.9), \quad(\mathrm{V} 1, \mathrm{~V} 2)=(0.6,-0.8)
$$

$$
10 \%
$$

Use the table-look-up method to simulate random variables $X$ from $U(0,1)$.
Where the p.d.f of $X$ is: $f(x)=\log _{e} x$ (implicit form)
(Hint: see page 95)
Simulate the random variable X with the following probabilities:
(Hint: see page 93)

From a $\mathrm{U}(0,1)$ in the following table:
$10 \%$

5- Simulate a Binomial random variable $X$ with $B(9,0.72)$ from a set of uniform random variables $\mathrm{U}(0,1)$, by using Bernouli random variable, where:

$$
\mathrm{U} 1=0.9, \mathrm{U} 2=0.7, \mathrm{U} 3=0.6, \mathrm{U} 4=0.2, \mathrm{U} 5=0.4, \mathrm{U} 6=0.5, \mathrm{U} 7=0.3, \mathrm{U} 8=0.8, \mathrm{U} 9=0.1
$$

(Hint: See page 82) $10 \%$

$$
\mathrm{p}=0.72
$$

6-Simulate random variable $X$ with geometric distribution and $p=0.8$ from $U(0,1)=0.9$

7- Simulate a Poisson distribution random variable, K , from the following exponential random variables: $\mathrm{E} 1=0.1, \mathrm{E} 2=0.7, \mathrm{E} 3=0.3, \mathrm{E} 4=0.2 \quad 10 \%$
(Hint: See page 84)
8- In randomized response technique (RRT), if we have $\mathrm{P}_{0}=0.5$, and $\operatorname{Pr}[\mathrm{N} \mid \mathrm{Yes}]=0.8$, and total probability from survey is: $\operatorname{Pr}[\mathrm{Yes}]=0.6$, find the $\operatorname{Pr}[\mathrm{E} \mid \mathrm{Yes}]=$ ? (Hint: See page 51) $10 \%$
9- Describe control variates in the variance reduction techniques. $5 \%$

| I | 0 | 1 | 2 | 3 | 4 | 5 | 6 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\operatorname{Pr}[\mathrm{X}<\mathrm{I}]$ | 0.01 | 0.21 | 0.31 | 0.48 | 0.56 | 0.58 | 0.62 |
| $\mathrm{X}=\ldots \log _{\mathrm{e}} \ldots-\ldots$ |  |  |  |  |  |  |  |
| $\operatorname{Pr}[\mathrm{E} \mid \mathrm{Yes}]=$ |  |  |  |  |  |  |  |
| $(\mathrm{N} 1, \mathrm{~N} 2)=$ | ,$(\mathrm{N} 1, \mathrm{~N} 2)=$ |  |  |  |  |  |  |

## EMBED Equation. 3

```
X=
X=
    U Ullllllll
    X
K=
x(0)=0,x(1)= ,x(2)= ,x(3)= ,x(4)= ,x(5)= ,x(6)= ,x(7)=
```

