

Simulation Exam Name: University of the Ryukyus
3-rd year undergraduate No: Faculty of Engineering
2005-2-14 Department of Information Eng.
Time: 90 minutes (write answers in boxes) Prof. M.R. Asharif

1- In randomised response technique (RRT), if we have $p_0=0.4$, $\Pr[\text{Yes}|N]=0.7$,
and total probability from survey is: $\Pr[\text{Yes}]=0.7$, find the $\Pr[\text{Yes}|E]=?$
(Hint: See page 51) 10%

2- For the following two dimensional transformation:

$$w=x-y$$

$$z=x+y$$

Find the joint pdf of $f(w,z)$, if the the joint pdf of $f(x,y)$, has the following Normal distribution:

EMBED Equation.3

(Hint: See page 35)

10%

3- In the mixed congruential generator: **EMBED Equation.3**

Simulate the first five numbers with seed **EMBED Equation.3** . Then find the correlation between two successive numbers.

5%

5%

(Hint: See page 60-61)

4- Simulate the normal distributed random variables (N1, N2) by using The Box-Muller method from the following U1, U2 uniform distributed random variables:

$$U1=0.3, U2=0.5$$

10%

(Hint: See page 78 Eq. 4.1)

5- Simulate the Gamma distributed random variables, G, with **EMBED Equation.3**

for $n=5$, EMBED Equation.3 from the following uniform distributed random variables, $U(0,1)$:

$U1=0.9, U2=0.7, U3=0.6, U4=0.2, U5=0.4$ 10%

(Hint: See page 82)

6- Two independent uniform random numbers with $U(0,1)$ are given in the binary form as below: $U1=0.10110110$

$U2=0.10111110$

Simulate the binomial distribution $B(8,1/2)$ random variables, $X1$, from $U1$ and $X2$, with $B(8,1/4)$ from $U1$ and $U2$. 10%

(Hint: See page 83)

7- Simulate a Poisson distribution random variable, K , with parameter EMBED Equation.3 from the following uniform random variables: $U1= 0.8, U2= 0.8, U3= 0.6, U4= 0.5$

10%

(Hint: See page 84)

8-Simulate the random variable X with the following probabilities:

(Hint: see page 93)

From a $U(0,1)$ in the following table:

10%

**9-Simulate random variable X with geometric distribution and $p=0.5$ from $U(0,1)$
=0.3**

(Hint: See page 93 Eq. 5.4)

10%

I	0	1	2	3	4	5	6
Pr [X<I]	0.2	0.3	0.6	0.7	0.9	0.92	0.95

X1=

X2=

EMBED Equation.3

X=

U	0.15	0.55	0.35	0.65	0.75	0.85	0.93
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X

x(0)=1, x(1)= ,x(2)= ,x(3)= ,x(4)= , x(5)=

Pr[Yes | E] =

f(w,z)=

N1= ,N2=

G=

K=