

Simulation Exam Name:
3-rd year undergraduate No:
2008-2-18 Last Term Examination
Eng.

University of the Ryukyus
Faculty of Engineering
Department of Information

Time: 90 minutes (write answers in boxes) Prof. M.R. Asharif

1- If the sequence $x(n)$ has the following properties:

$$x(0)=0, x(1)=x(2)=1$$

where: $x(n)=x(n-1)+x(n-2)-x(n-3)$ for $n \geq 3$

Then, find $x(100)$, by regression or simulation method. 10%

$x(100) =$

2- In randomised response technique (RRT), if we have:

$Pr[Yes]=0.7$ (total probability from survey).

$Pr[Yes|N]=0.8$ (answering probability to non-embarrassing question).

$Pr[Yes|E]=0.3$ (answering probability to embarrassing question).

Find: $1-p_0$ (condition for answering to embarrassing question).

(Hint: See page 51)

10%

$1-p_0 =$

3- In the following chaotic system:

10%

$$x(n+1)=4 r x(n) [1-x(n)]$$

If $r=0.7$, find the attractor of this chaotic system by simulation or direct computation.

(Hint: See chap. 6)

$x(\infty) =$

4- Simulate the normal distributed random variables ($N1, N2$) by using Box-Muller method from the following pair of uniform distributed random variables: $(U1, U2)=(0.9, 0.2)$ (Hint: See page 78 use Eq. 4.1)

10%

$(N1, N2) =$

5- Simulate the Gamma distributed random variables, G , with $\Gamma(n, \lambda)$ for $n=4$, $\lambda = 0.25$ from the following uniform distributed random variables, $U(0,1)$:
 $U1=0.80, U2=0.90, U3=0.71, U3=0.72$ 10%
 (Hint: See page 82)

G=

6- Two independent uniform random numbers with $U(0,1)$ are given in the binary form as below: $U1=0.01010110$ 10%
 $U2=0.11010101$
 Simulate the binomial distribution $B(8,1/2)$ random variables, $X1$, from $U1$ and $X2$, with $B(8,1/4)$ from $U1$ and $U2$.
 (Hint: See page 83)

X1= X2=

7- Simulate a Poisson distribution random variable, K , with parameter $\lambda = 0.9$ from the following uniform random variables:
 $U1= 0.9, U2= 0.7, U3= 0.8, U4= 0.4$ (Hint: See page 84)
 10%

K=

8- Simulate random variable X with geometric distribution and $p=0.3$ from $U(0,1)=0.7$ 10%
 (Hint: See page 93 Eq. 5.4)

X=

9- Use the table-look-up method to simulate random variables X from $U(0,1)$. Where the p.d.f of X has Cauchy distribution as follows:
 $f(x)=1 / \pi(1+ x^2),$ 10%
 $-\infty < x < \infty$
 Also, find the value of X when $U=0.75$
 (Hint: see page 95-96)

X= X u=0.75 =
