

SYSTEM ARCHITECTURE  
ADVANCED SYSTEM ARCHITECTURE  
LUO Chapter 18.1 and 18.2



**Introduction to OFDM**

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2013/Fall-Winter Term  
Monday 12:50

Room# 1-322 or 5F Meeting Room  
Instructor: Fire Tom Wada, Professor



# What is OFDM?

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- OFDM  
=Orthogonal Frequency Division Multiplexing
- Many orthogonal sub-carriers are multiplexed in one symbol
  - What is the orthogonal?
  - How multiplexed?
  - What is the merit of OFDM?
  - What kinds of application?



# Outline

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- Background, history, application
- Review of digital modulation
- FDMA vs. Multi-carrier modulation
- Theory of OFDM
- Multi-path
- Real OFDM systems examples



# Why OFDM is getting popular?

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- State-of-the-art high bandwidth digital communication start using OFDM
  - Terrestrial Video Broadcasting in Japan and Europe
    - ISDB-T / DVB-T
  - ADSL High Speed Modem
  - WLAN such as IEEE 802.11a/g/n/ac
  - WiMAX as IEEE 802.16d/e
- Economical OFDM implementation become possible because of advancement in the LSI technology



# Brief history of OFDM

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- First proposal in 1950's
- Theory completed in 1960's
- DFT implementation proposed in 1970's
- Europe adopted OFDM for digital radio broadcasting in 1987
- OFDM for Terrestrial Video broadcasting in Europe and Japan
- ADSL, WLAN(802.11a)



# Digital modulation basics

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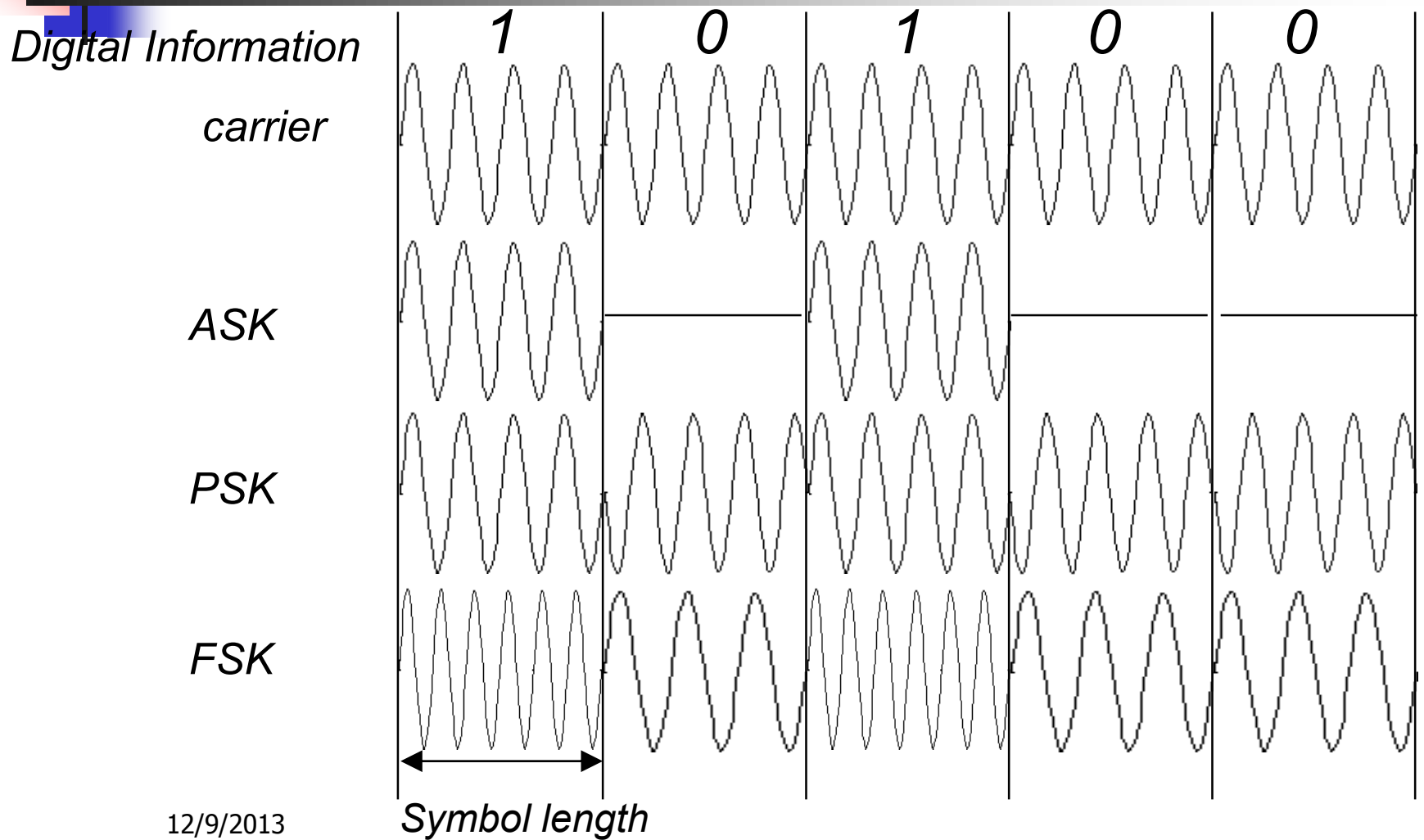
- Digital modulation modulates three parameters of sinusoidal signal.

- $A, \theta_k, f_c,$   
$$s(t) = A \cdot \cos(2\pi \cdot f_c \cdot t + \theta_k)$$

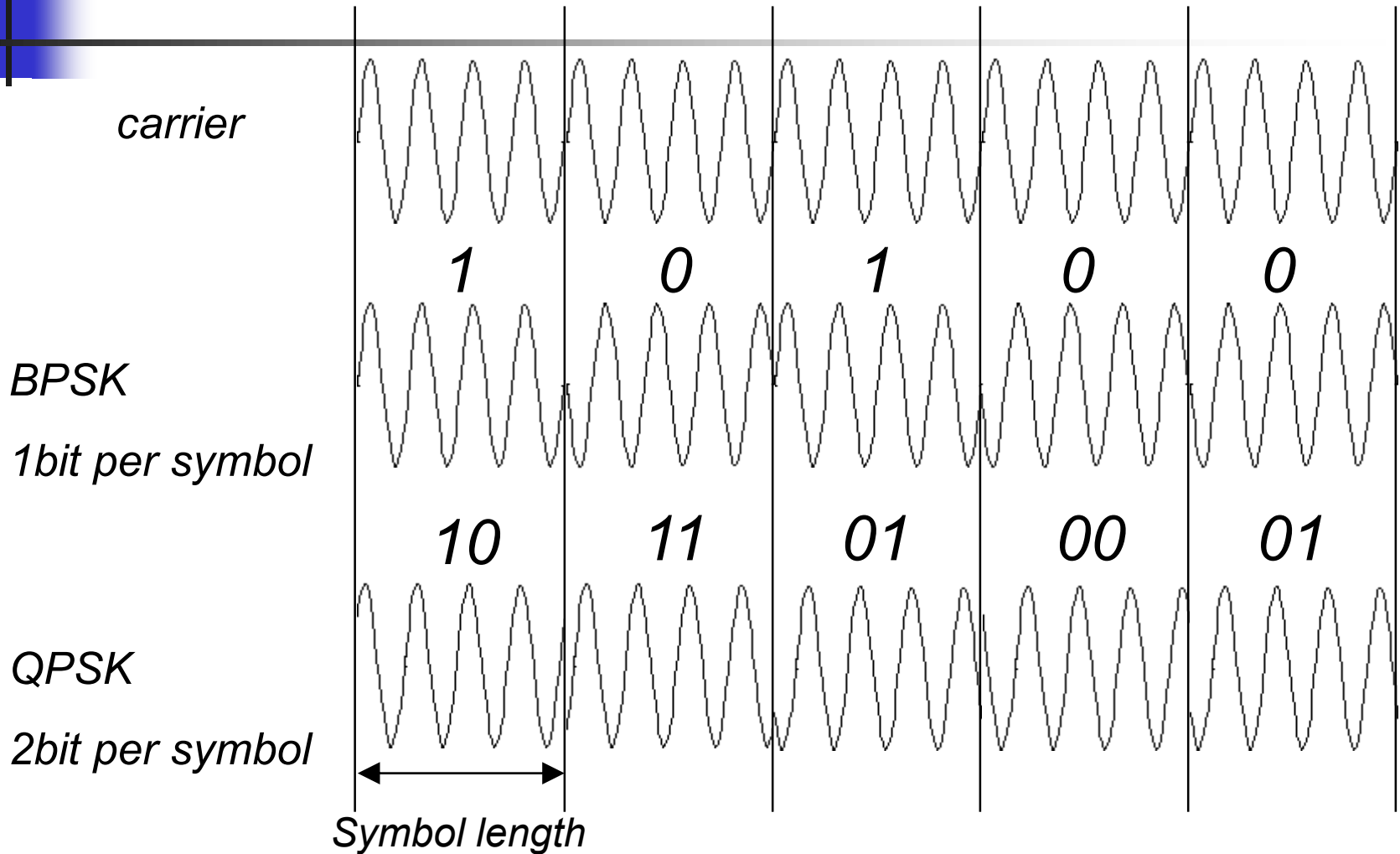
- Three type digital modulation:
  - ASK : Amplitude Shift Keying
  - PSK : Phase Shift Keying
  - FSK : Frequency Shift Keying

***OFDM uses combination of ASK and PSK such as QAM, PSK***

# Symbol Waveform



# Multi bit modulation





# Mathematical expression of digital modulation

- Transmission signal can be expressed as follows

$$\begin{aligned} s(t) &= \cos(2\pi \cdot f_c \cdot t + \theta_k) \\ &= \cos\theta_k \cdot \cos(2\pi \cdot f_c \cdot t) - \sin\theta_k \cdot \sin(2\pi \cdot f_c \cdot t) \end{aligned}$$

$$a_k = \cos\theta_k, \quad b_k = \sin\theta_k$$

$$s(t) = \text{Re}[(a_k + jb_k)e^{j2\pi f_c t}]$$

- $s(t)$  can be expressed by complex base-band signal  $(a_k + jb_k)e^{j2\pi f_c t}$

$e^{j2\pi f_c t}$  *Indicates carrier sinusoidal*

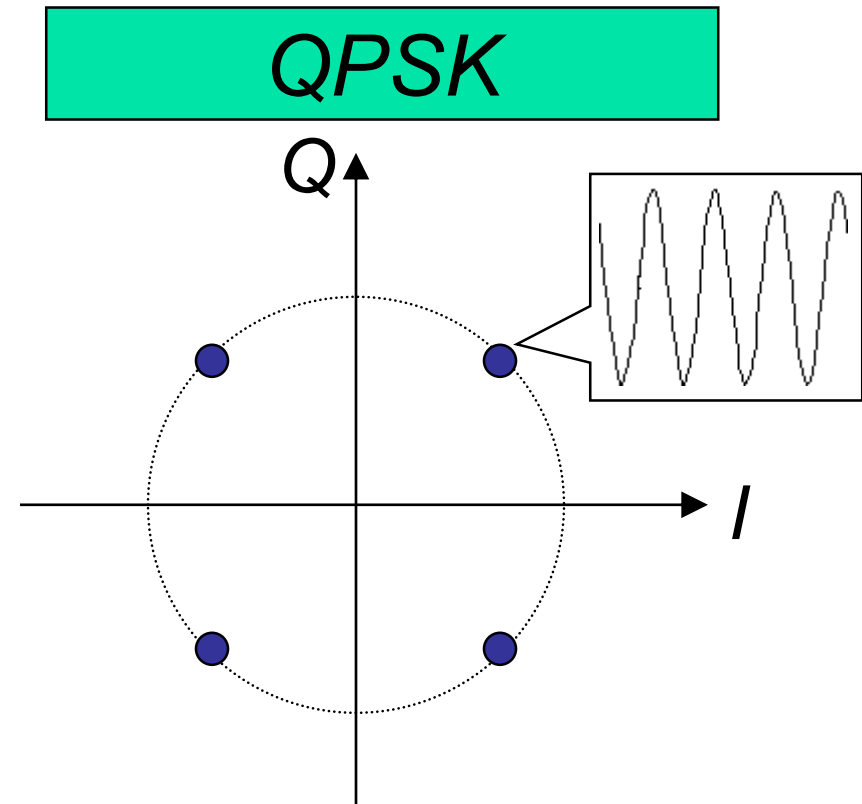
$(a_k + jb_k)$  *Digital modulation*

**Digital modulation can be expressed by the complex number**

# Constellation map

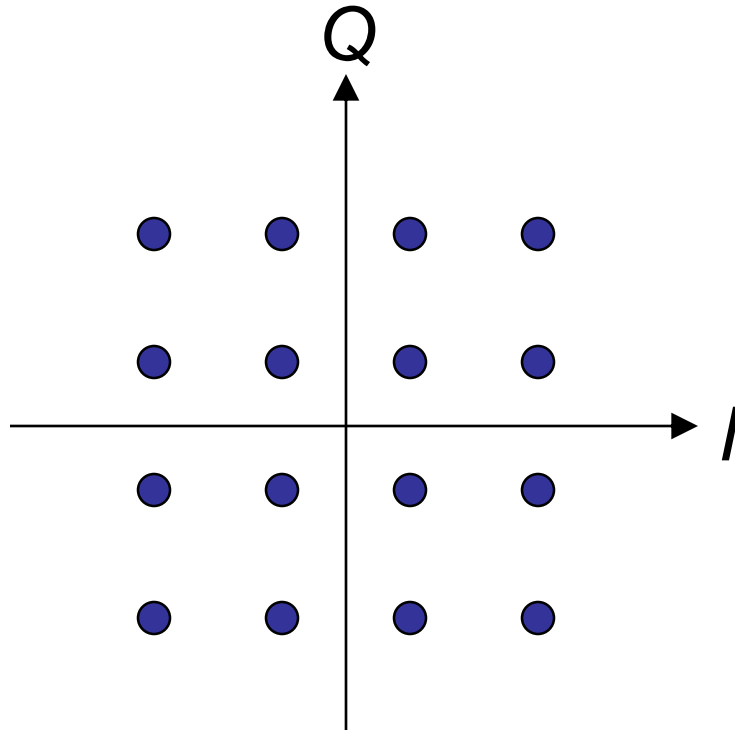
- $(a_k + jb_k)$  is plotted on I(real)-Q(imaginary) plane

data		$a_k$	$b_k$
00	$\pi/4$	$\frac{1}{\sqrt{2}}$	$\frac{1}{\sqrt{2}}$
01	$3\pi/4$	$-\frac{1}{\sqrt{2}}$	$\frac{1}{\sqrt{2}}$
11	$5\pi/4$	$-\frac{1}{\sqrt{2}}$	$-\frac{1}{\sqrt{2}}$
10	$7\pi/4$	$\frac{1}{\sqrt{2}}$	$-\frac{1}{\sqrt{2}}$

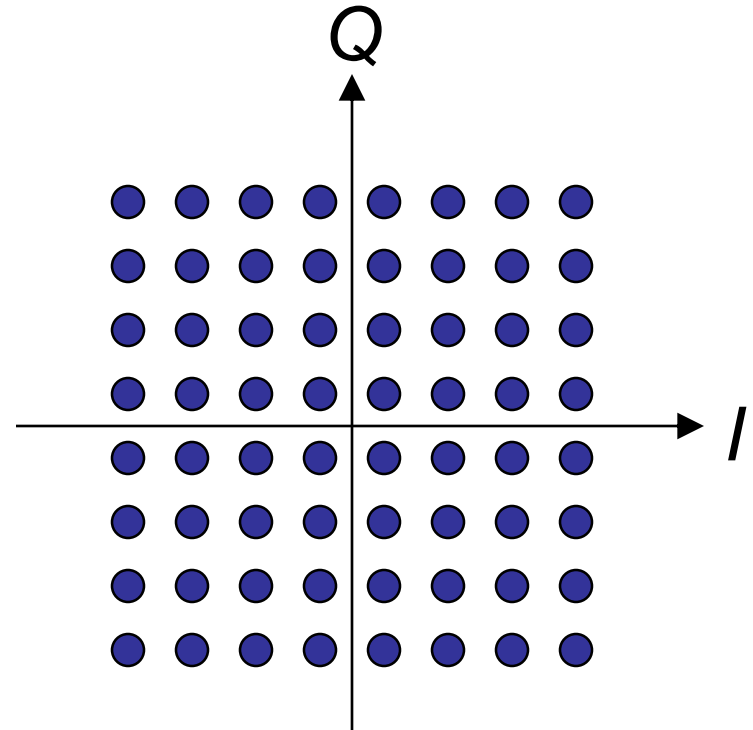


# Quadrature Amplitude Modulation (QAM)

16QAM



64QAM

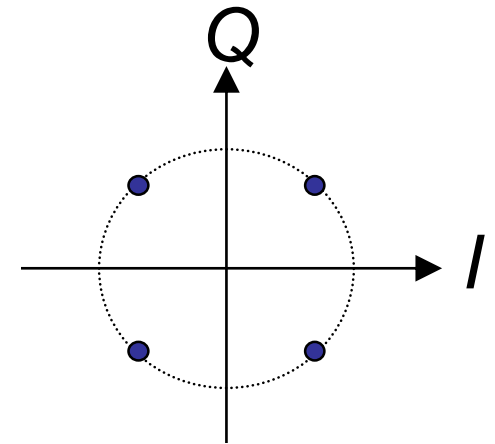


# Summary of digital modulation

- Type of modulation: ASK,PSK,FSK,QAM
- OFDM uses ASK,PSK,QAM
- Digital modulation is mathematically characterized by the coefficient of complex base-band signal

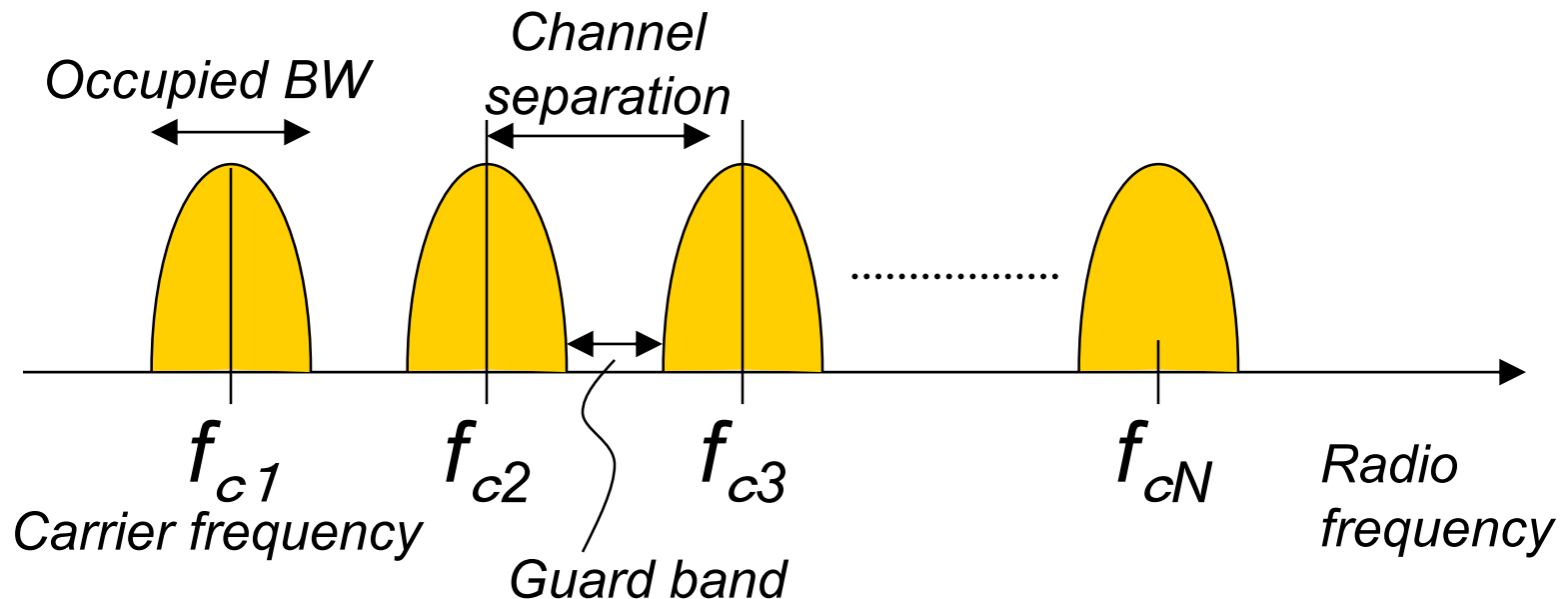
$$(a_k + jb_k)$$

- Plot of the coefficients gives the constellation map



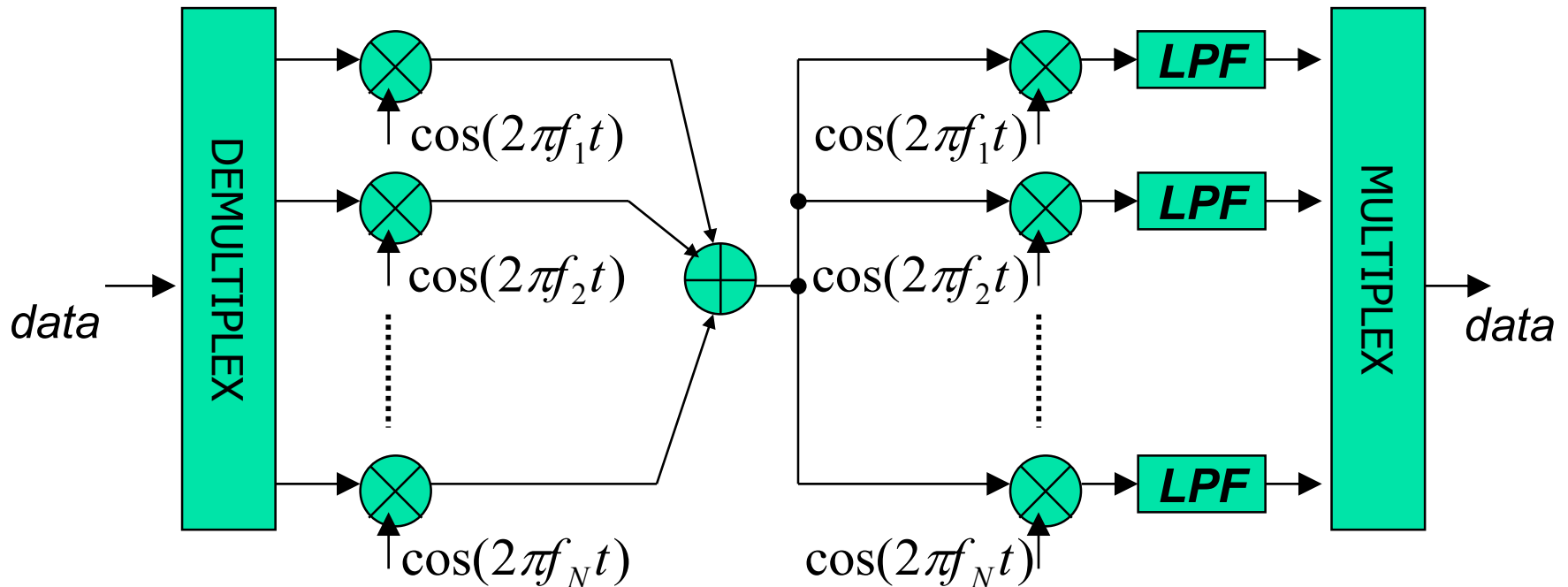
# Frequency Division Multiple Access (FDMA)

- Old conventional method (Analog TV, Radio etc.)
- Use separate carrier frequency for individual transmission

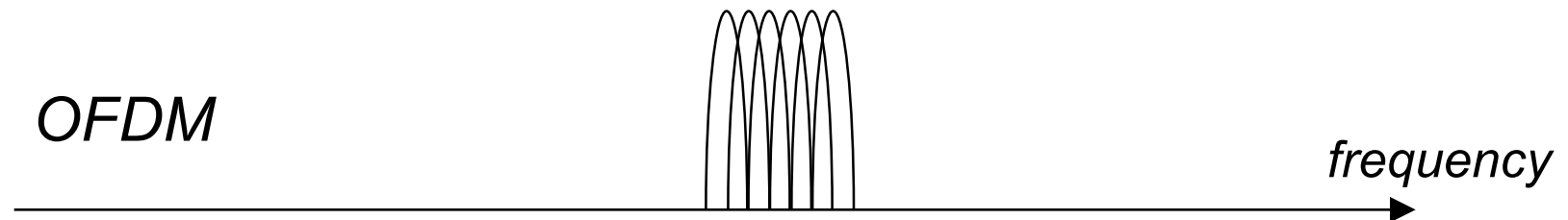
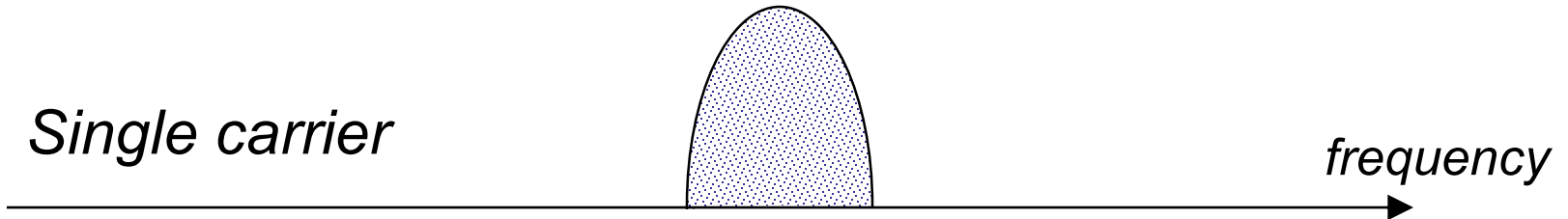
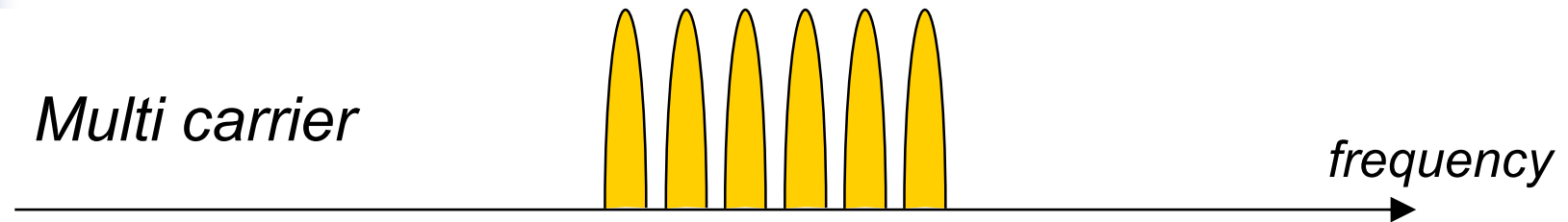


# Multi-carrier modulation

- Use multiple channel (carrier frequency) for one data transmission



# Spectrum comparison for same data rate transmission





# OFDM vs. Multi carrier

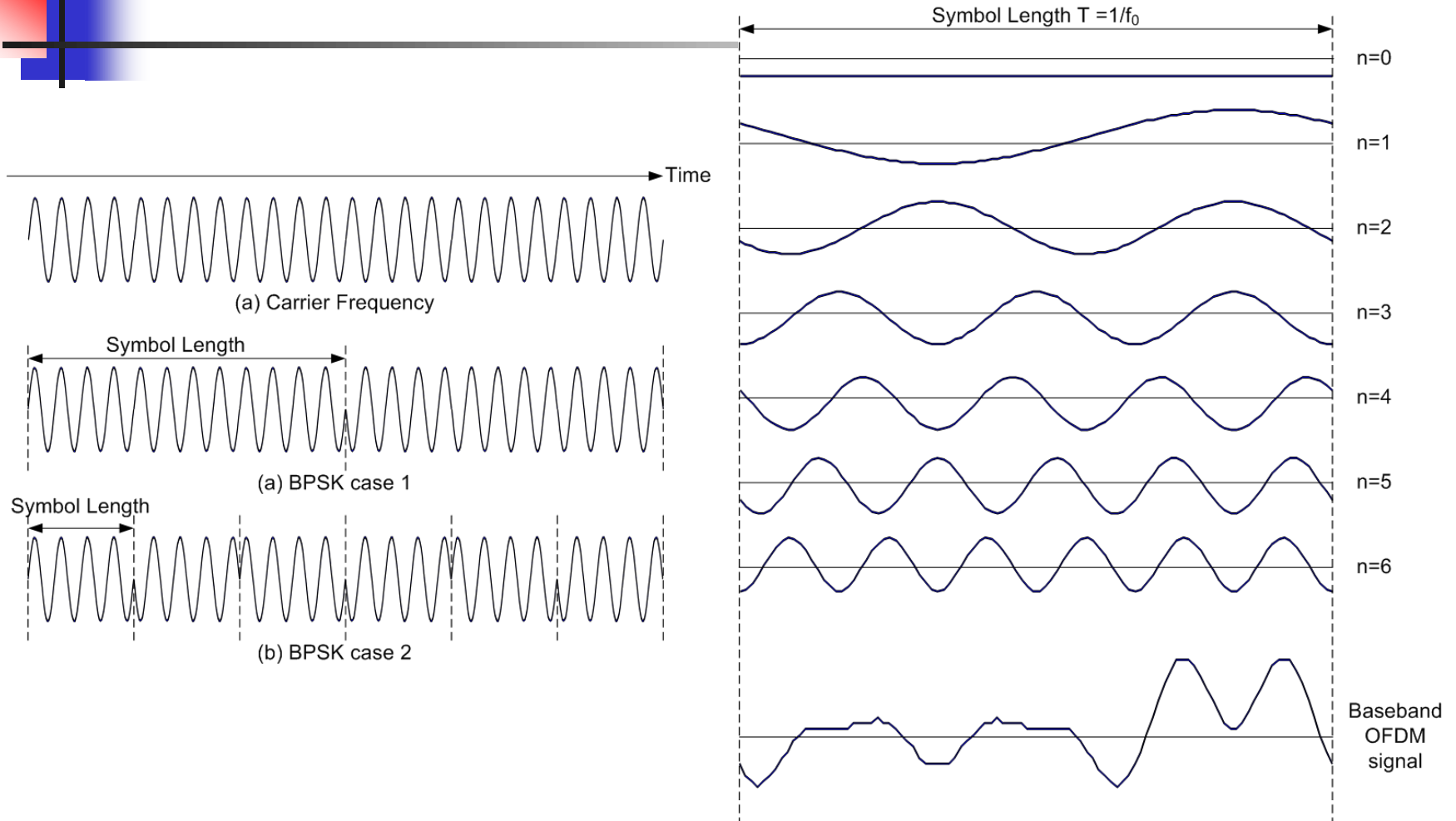
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- OFDM is multi carrier modulation
- OFDM sub-carrier spectrum is overlapping
- In FDMA, band-pass filter separates each transmission
- In OFDM, each sub-carrier is separated by DFT because carriers are orthogonal
  - Condition of the orthogonality will be explained later
- Each sub-carrier is modulated by PSK, QAM

***Thousands of PSK/QAM symbol can be simultaneously transmitted in one OFDM symbol***

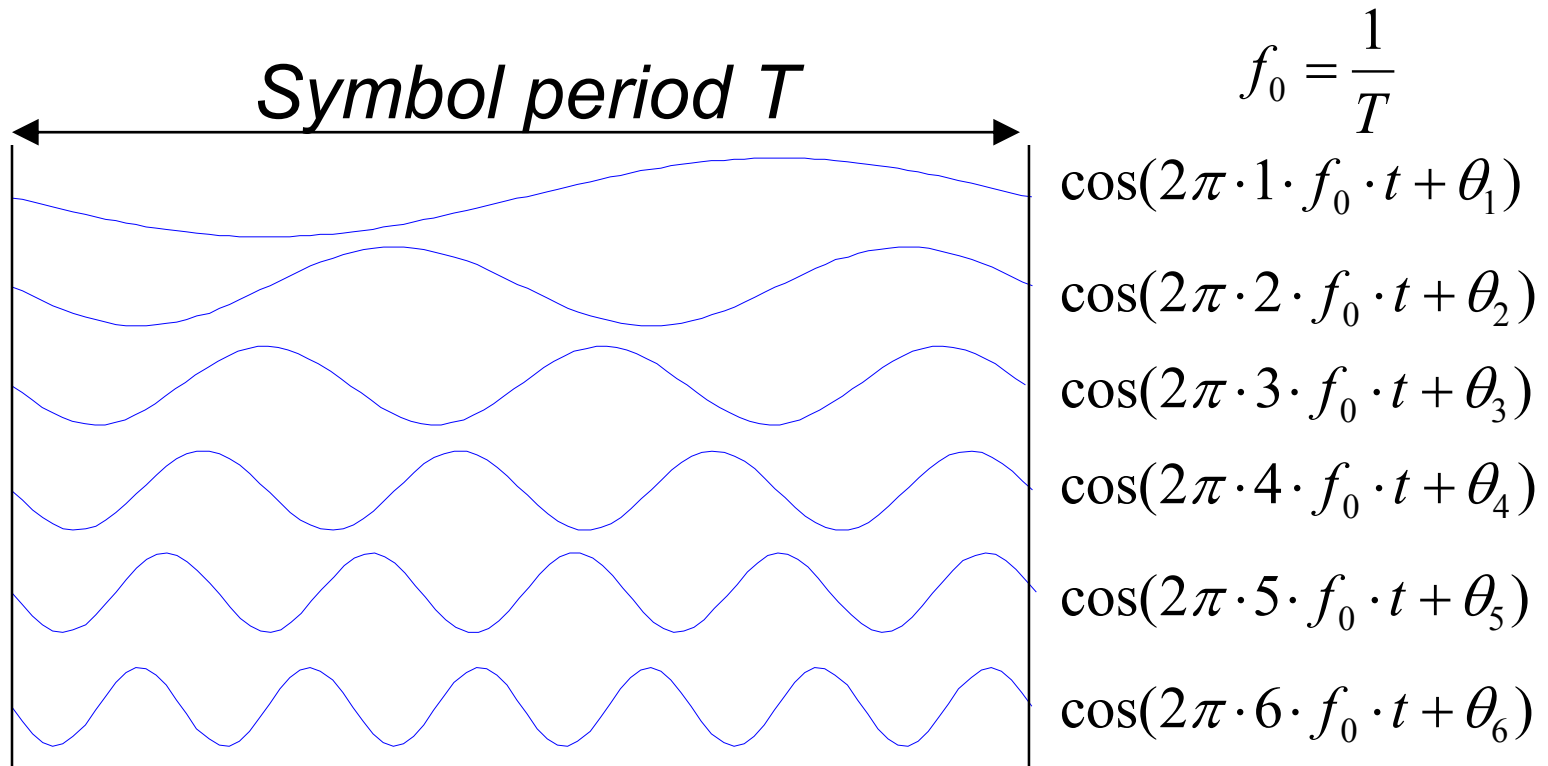


# Single Carrier vs. Multi Carrier



# OFDM carriers

- OFDM carrier frequency is  $n \cdot 1/T$





# Sinusoidal Orthogonality

- $m, n$ : integer,  $T=1/f_0$

$$\int_0^T \cos(2\pi m f_0 t) \cdot \cos(2\pi n f_0 t) dt = \begin{cases} \frac{T}{2} & (m = n) \\ 0 & (m \neq n) \end{cases} \rightarrow \text{Orthogonal}$$

$$\int_0^T \sin(2\pi m f_0 t) \cdot \sin(2\pi n f_0 t) dt = \begin{cases} \frac{T}{2} & (m = n) \\ 0 & (m \neq n) \end{cases} \rightarrow \text{Orthogonal}$$

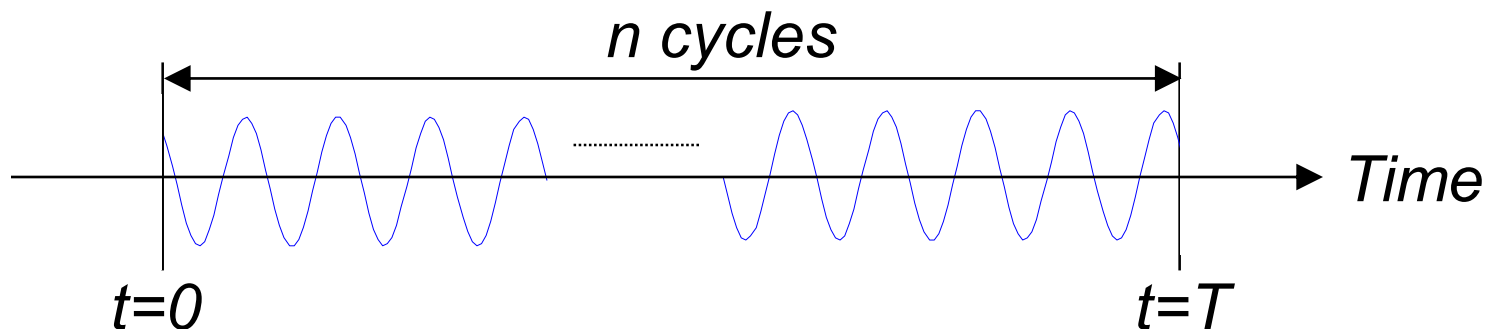
$$\int_0^T \cos(2\pi m f_0 t) \cdot \sin(2\pi n f_0 t) dt = 0 \rightarrow \text{Orthogonal}$$

# A sub-carrier of $f=nf_0$

$$a_n \cdot \cos(2\pi n f_0 t) - b_n \cdot \sin(2\pi n f_0 t)$$

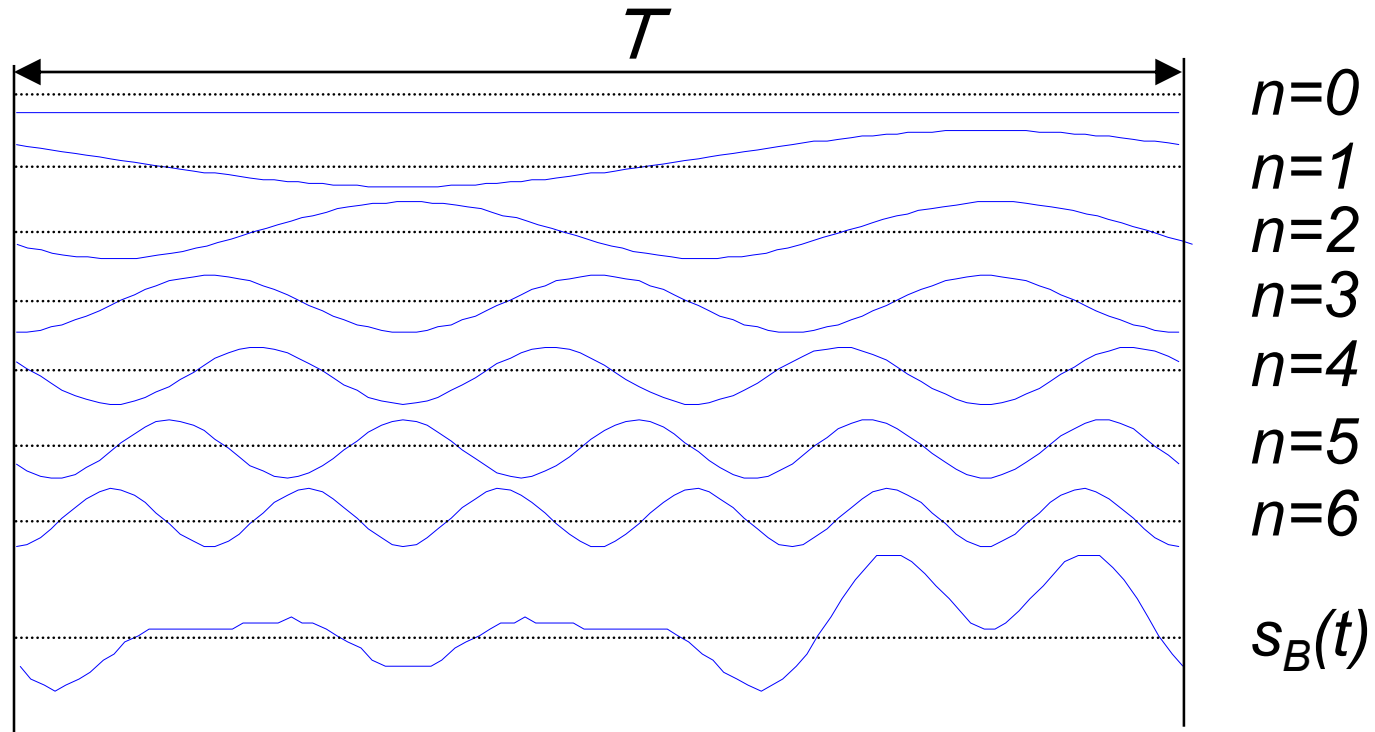
$$= \sqrt{a_n^2 + b_n^2} \cos(2\pi n f_0 t + \phi_n), \quad \phi_n = \tan^{-1} \frac{b_n}{a_n}$$

- Amplitude and Phase will be digitally modulated



# Base-band OFDM signal

$$s_B(t) = \sum_{n=0}^{N-1} \{a_n \cos(2\pi n f_0 t) - b_n \sin(2\pi n f_0 t)\}$$





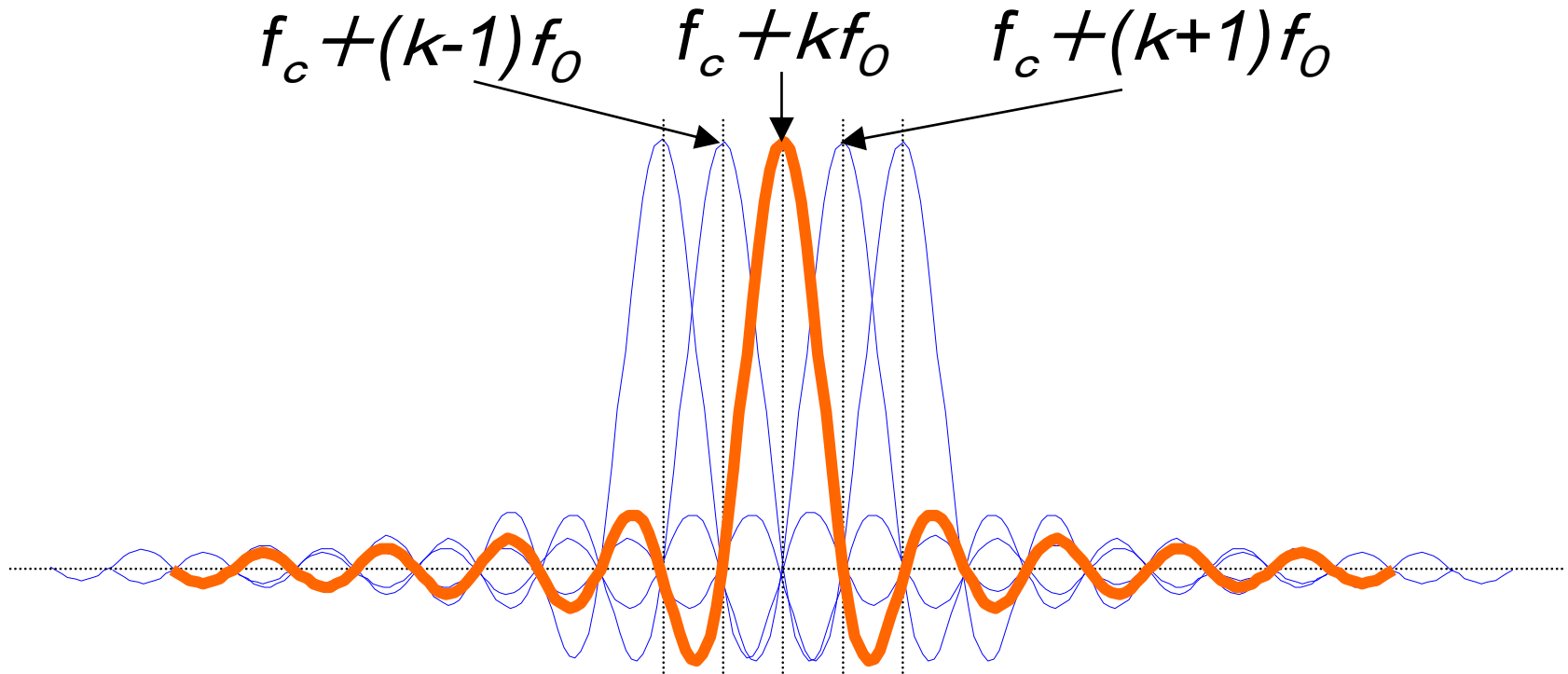
# Pass-band OFDM signal

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- $S_B(t)$  is upconverted to pass-band signal  $S(t)$
- $f_c$  frequency shift

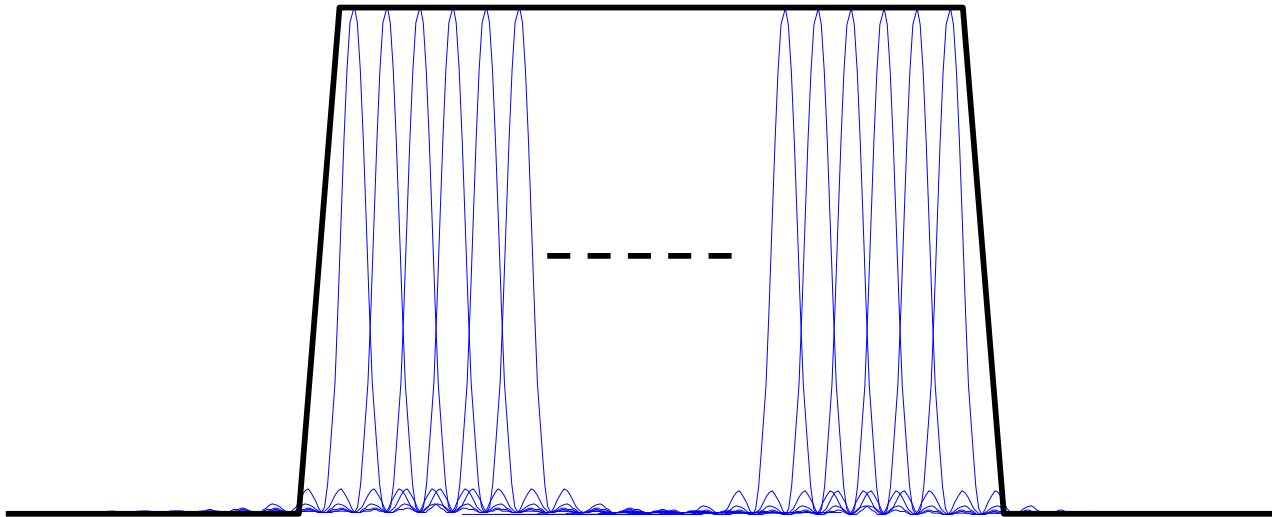
$$s(t) = \sum_{n=0}^{N-1} \left[ a_n \cos\{2\pi(f_c + nf_0)t\} - b_n \sin\{2\pi(f_c + nf_0)t\} \right]$$

# Actual OFDM spectrum



# OFDM power spectrum

- Total Power spectrum is almost square shape







# OFDM signal generation

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$$s(t) = \sum_{n=0}^{N-1} \left[ a_n \cos\{2\pi(f_c + nf_0)t\} - b_n \sin\{2\pi(f_c + nf_0)t\} \right]$$

- Direct method needs
  - N digital modulators
  - N carrier frequency generator
  - ➔ Not practical
- In 1971, method using DFT is proposed to OFDM signal generation

# OFDM signal generation in digital domain

- Define complex base-band signal  $u(t)$  as follows

$$s_B(t) = \text{Re}[u(t)]$$

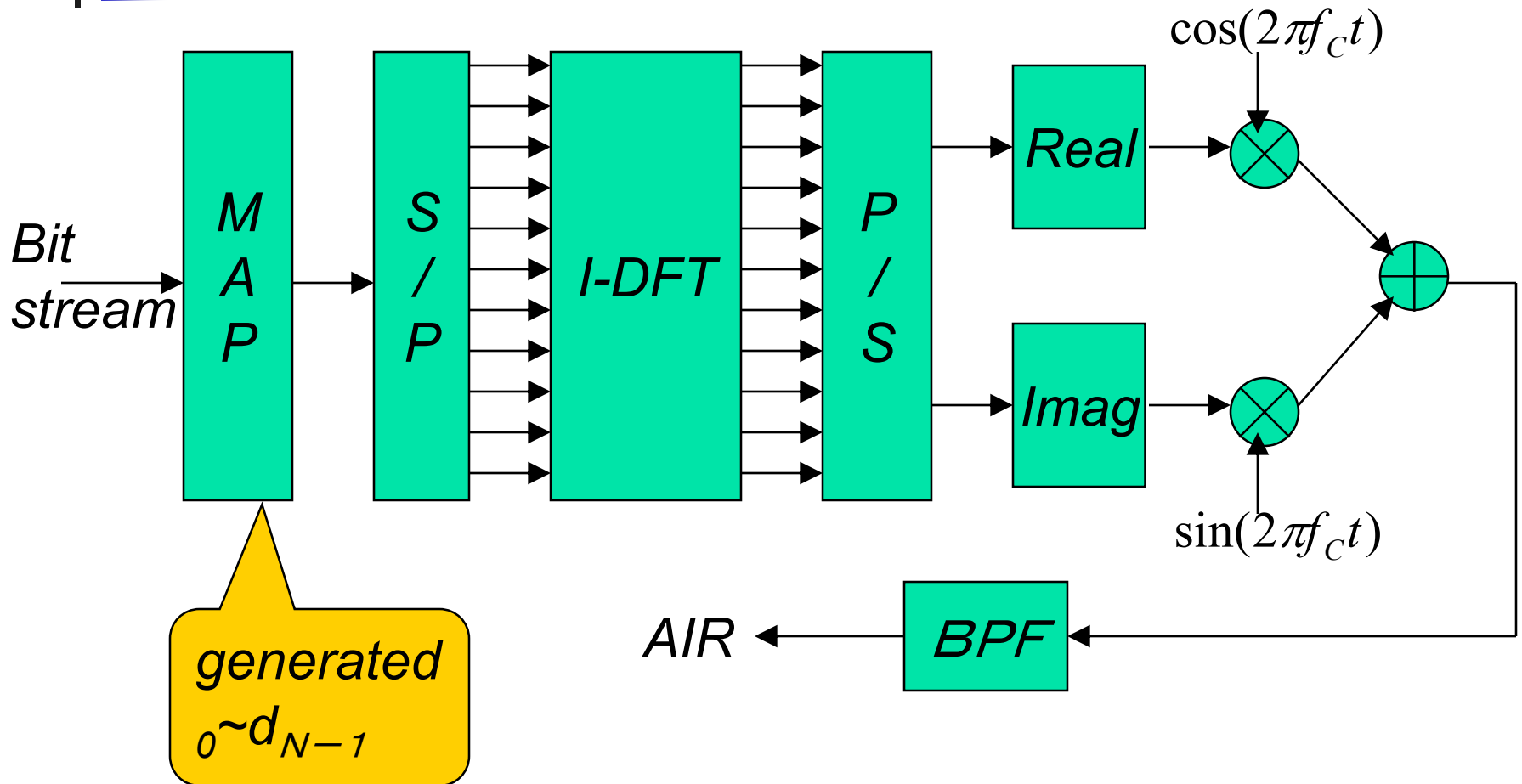
$$u(t) = \sum_{n=0}^{N-1} d_n \cdot e^{j2\pi n f_0 t}, \quad d_n = a_n + j b_n$$

- Perform  $N$  times sampling in period  $T$

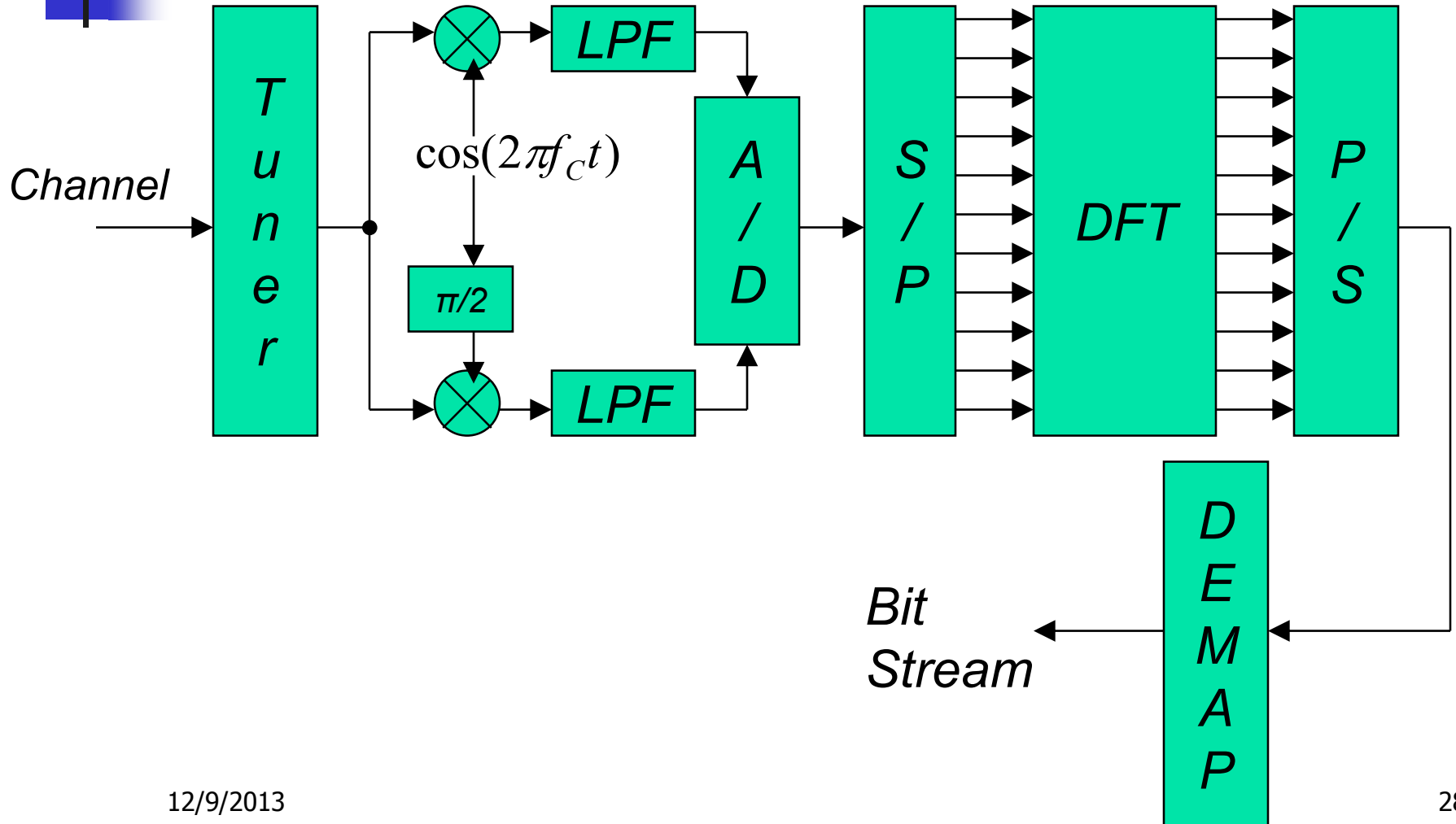
$$\begin{aligned} u\left(\frac{k}{Nf_0}\right) &= \sum_{n=0}^{N-1} d_n \cdot e^{j2\pi n f_0 \frac{k}{Nf_0}} = \sum_{n=0}^{N-1} d_n \cdot e^{j\frac{2\pi n k}{N}} \\ &= \sum_{n=0}^{N-1} d_n \cdot \left(e^{j\frac{2\pi}{N}}\right)^{nk} \quad (k = 0, 1, 2, \dots, N-1) \end{aligned}$$

$$u(k) = \text{IFFT}(d_n) = \text{IFFT}(a_n + j b_n)$$

# OFDM modulator

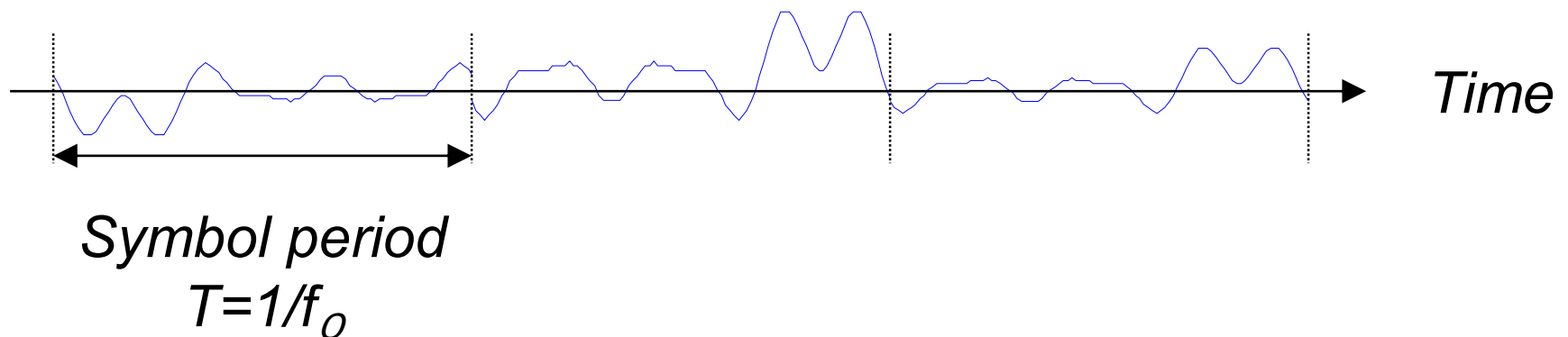


# OFDM demodulator (Too simple)



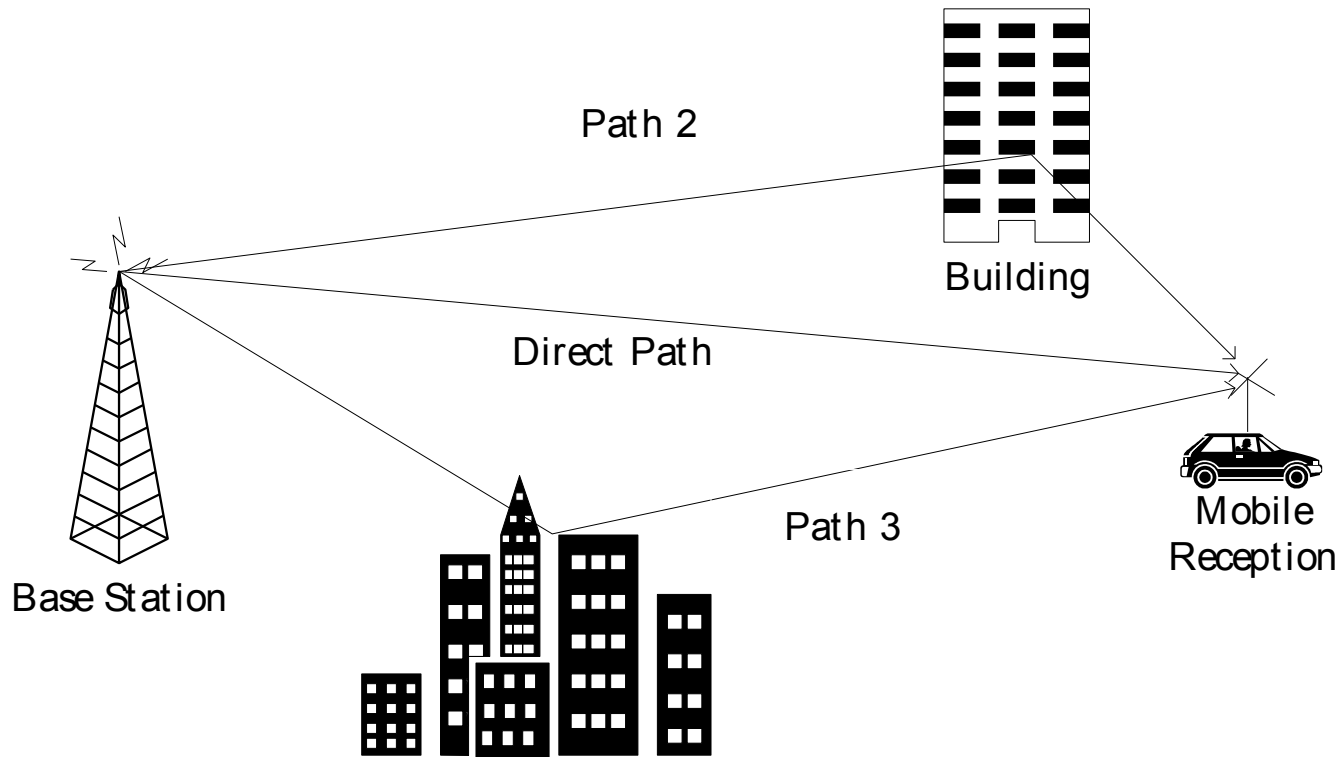
# Summary of OFDM signal

- Each symbol carries information
- Each symbol wave is sum of many sinusoidal
- Each sinusoidal wave can be PSK, QAM modulated
- Using IDFT and DFT, OFDM implementation became practical



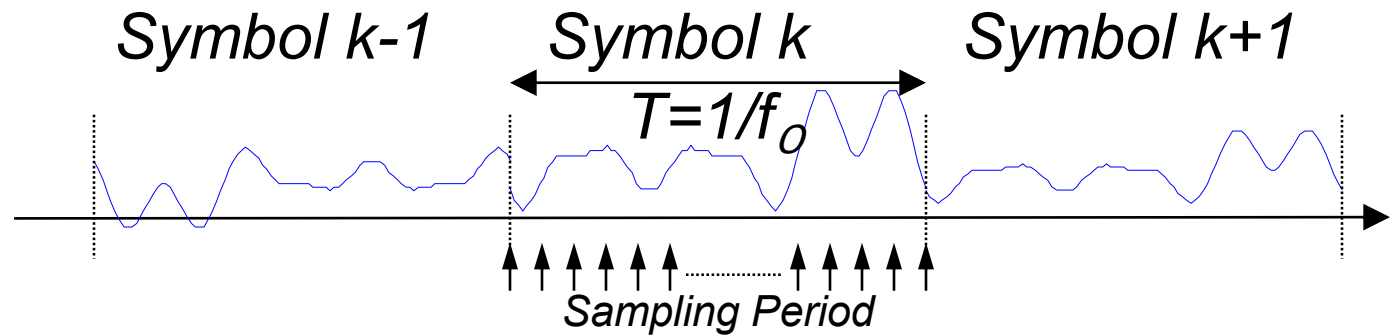
# Multi-path

- Delayed wave causes interference

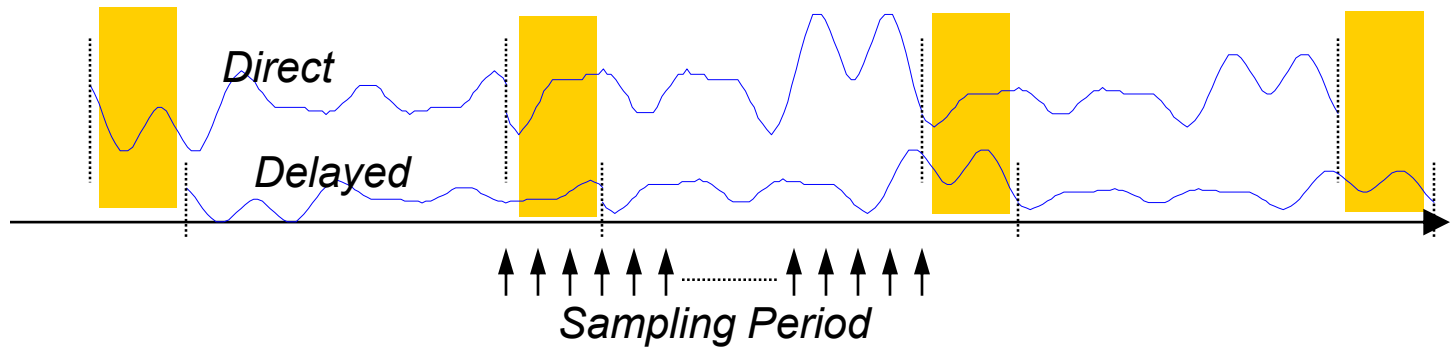


# Multi-pass effect

No multi-path

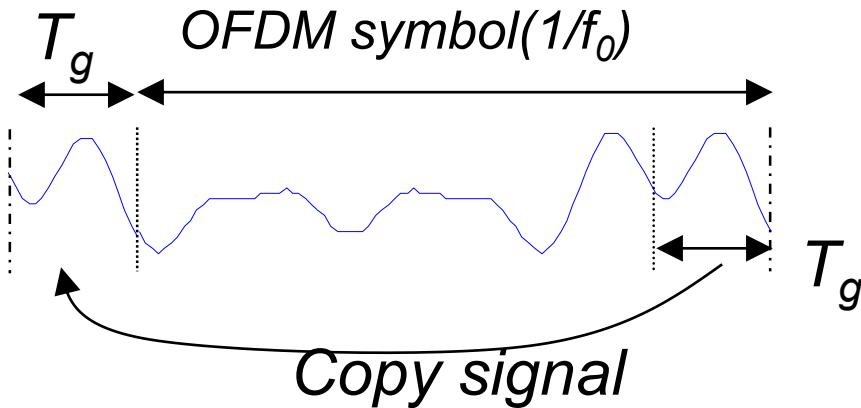


Multi-path

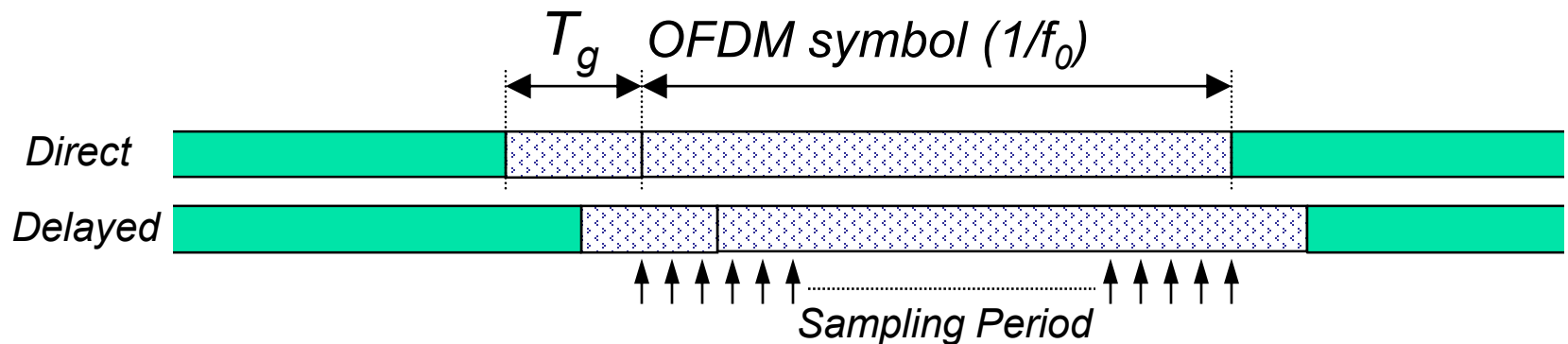


- Inter symbol interference (ISI) happens in Multi-path condition

# Guard Interval $T_g$



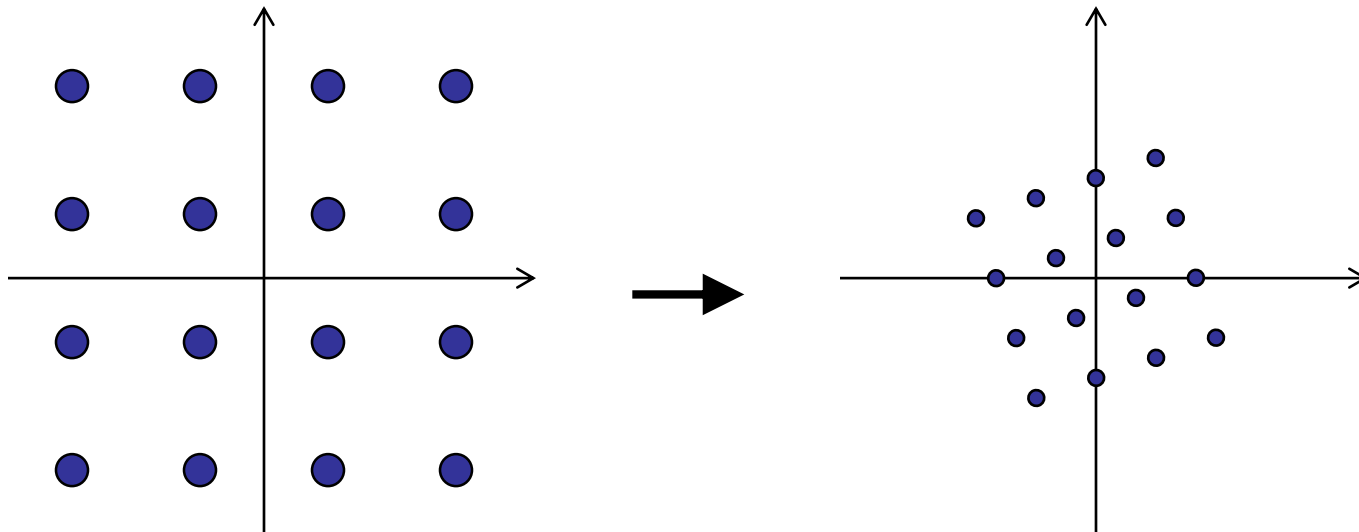
- By adding the Guard Interval Period, ISI can be avoided





# Multi-path

- By adding GI, orthogonality can be maintained
- However, multi-path causes Amplitude and Phase distortion for each sub-carrier
- The distortion has to be compensated by Equalizer



# 18.2.5

## Channel Estimation and Equalizer

- Reception signal  $s_R(t)$  
$$s_R(t) = \int_{-\infty}^{\infty} h(u)s(t-u)du + n_c(t) \quad (18.18)$$

- CTF 
$$H(f) = \int_0^{Tg} h(t)e^{-j2\pi ft}dt \quad (18.19)$$

- Frequency domain 
$$x(k,l) = H(f_c + lf_0)d(k,l) + N_B(k,l) \quad (18.20)$$

- Equalization 
$$\begin{aligned} \hat{d}(k,l) &= \frac{x(k,l)}{H(f_c + lf_0)} \\ &= d(k,l) + \frac{N_B(k,l)}{H(f_c + lf_0)} \end{aligned} \quad (18.21)$$

## 18.2.6

# OFDM communication and broadcasting systems

Application of OFDM	Effective OFDM symbol length $1/f_0$
WLAN (802.11g/a/n)	3.2us
XGP (eXtended Global Platform)	26.67us
3.9G mobile phone LTE	66.67 us
WiMAX (802.16e)	102.4us
3.9G mobile phone LTE (Extended mode)	133.33 us
China Digital TV Broadcasting DTMB	500.0us
Europe Digital TV Broadcasting DVB-T	896us (8K mode)
Japan Digital TV Broadcasting ISDB-T	1008us (8K mode)

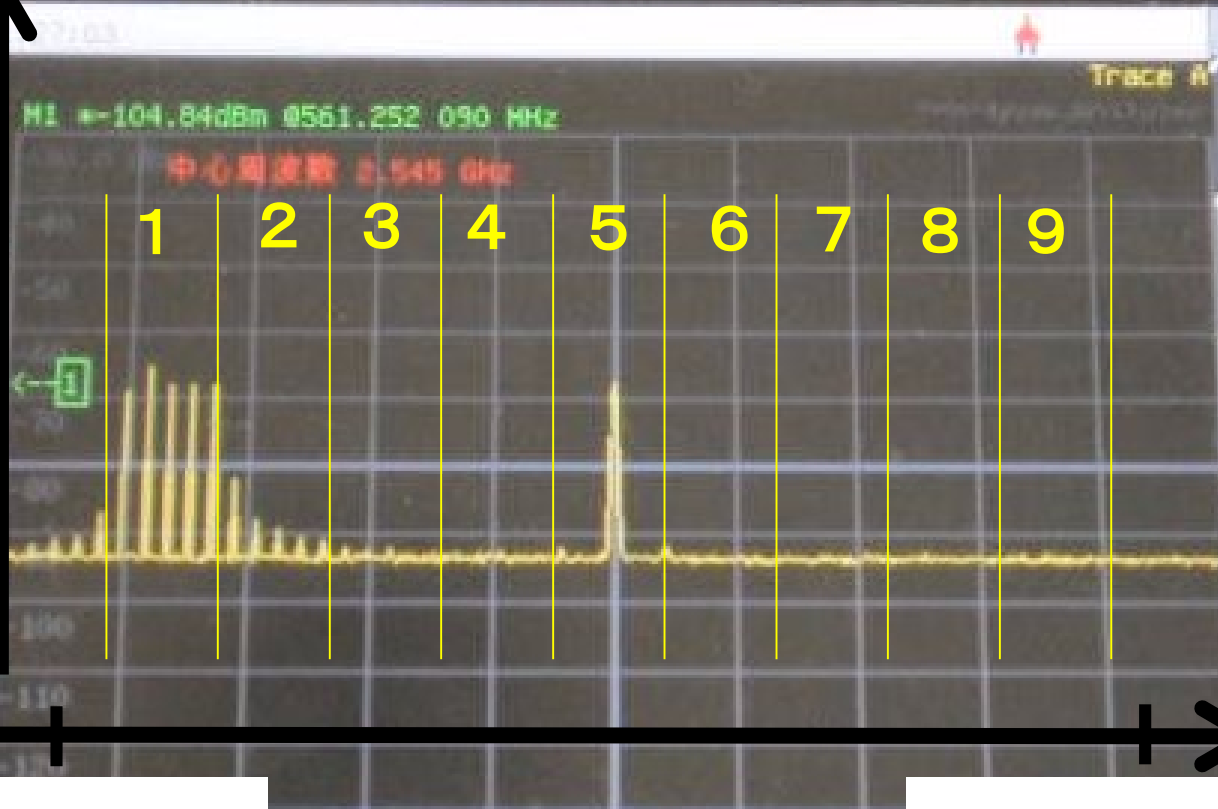
# OFDM system Measurement

Signal Analyzer

OFDM Communication System

# Signal Analyzer

Power



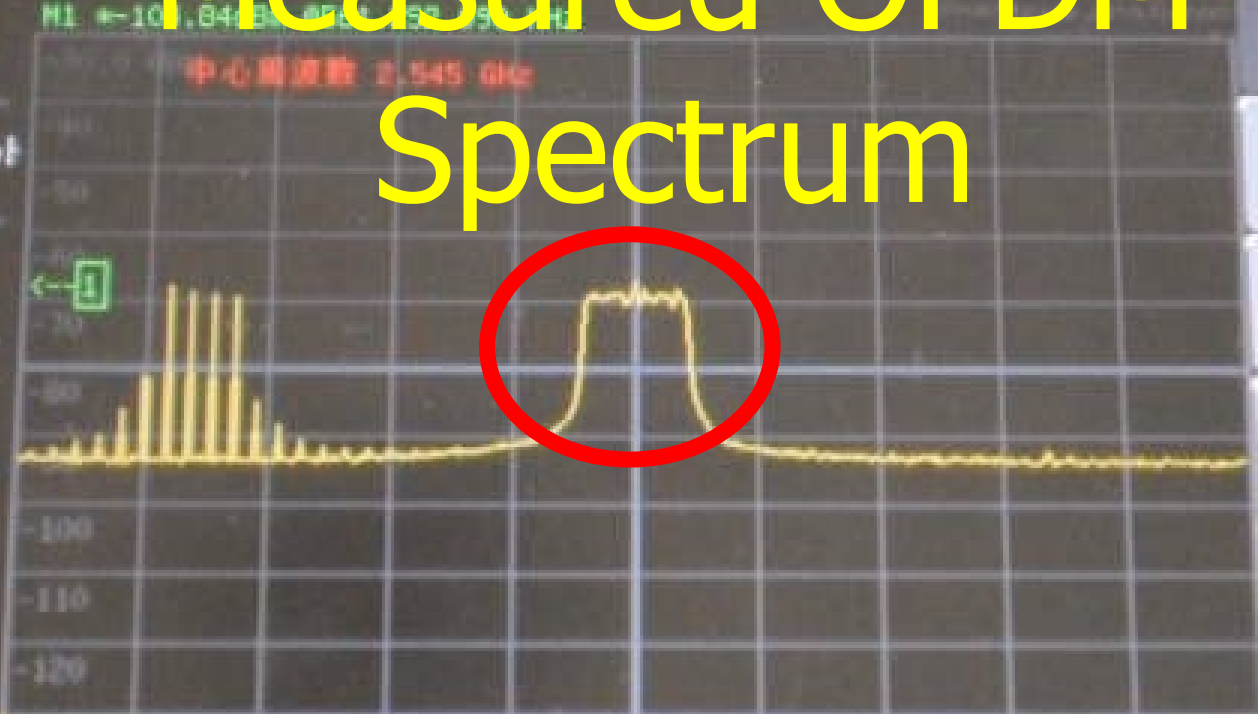
Frequency

2540  
Mega Hz

2550  
Mega Hz

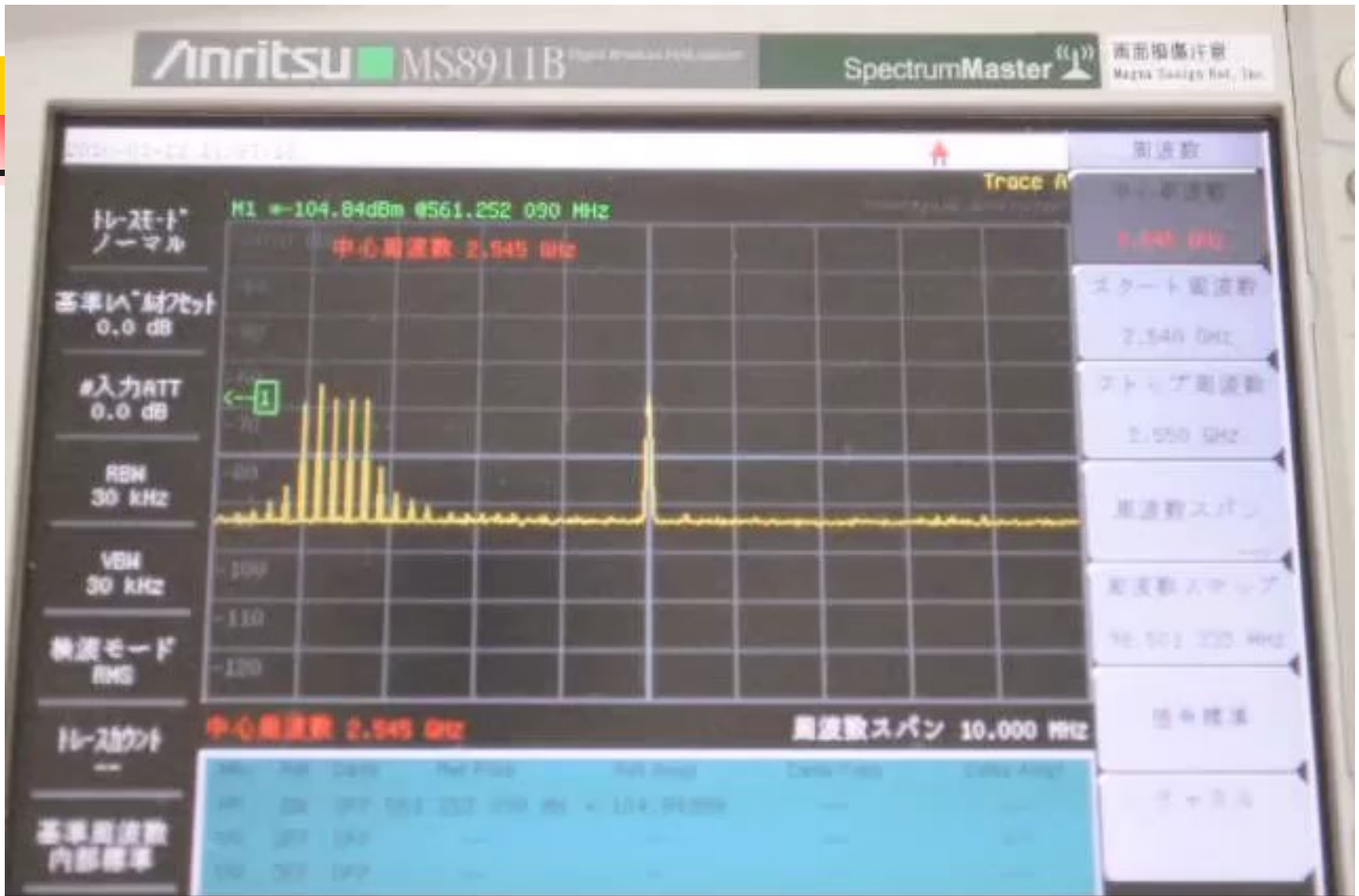


# Measured OFDM Spectrum



Ch	Mod	Const	Mod Freq	Mod Amp	Data Freq	Data Amp
M1	ON	QPSK	561.252 000 MHz	-104.84dBm	---	---
M2	OFF	QPSK	---	---	---	---
M3	OFF	QPSK	---	---	---	---

# Video Demo





# That's all for introduction

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- Feature of OFDM

1. High Frequency utilization by the square spectrum shape
2. Multi-path problem is solved by GI
3. Multiple services in one OFDM by sharing sub-carriers (3 services in ISDB-T)
4. SFN
5. Implementation was complicated but NOW possible because of LSI technology progress





# REAL OFDM SYSTEMS

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1. OFDM WLAN
2. OFDMA transceiver design (LTE)



# EXAMPLE 1)

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**WLAN**

**Wireless LAN**

**802.11a/g**

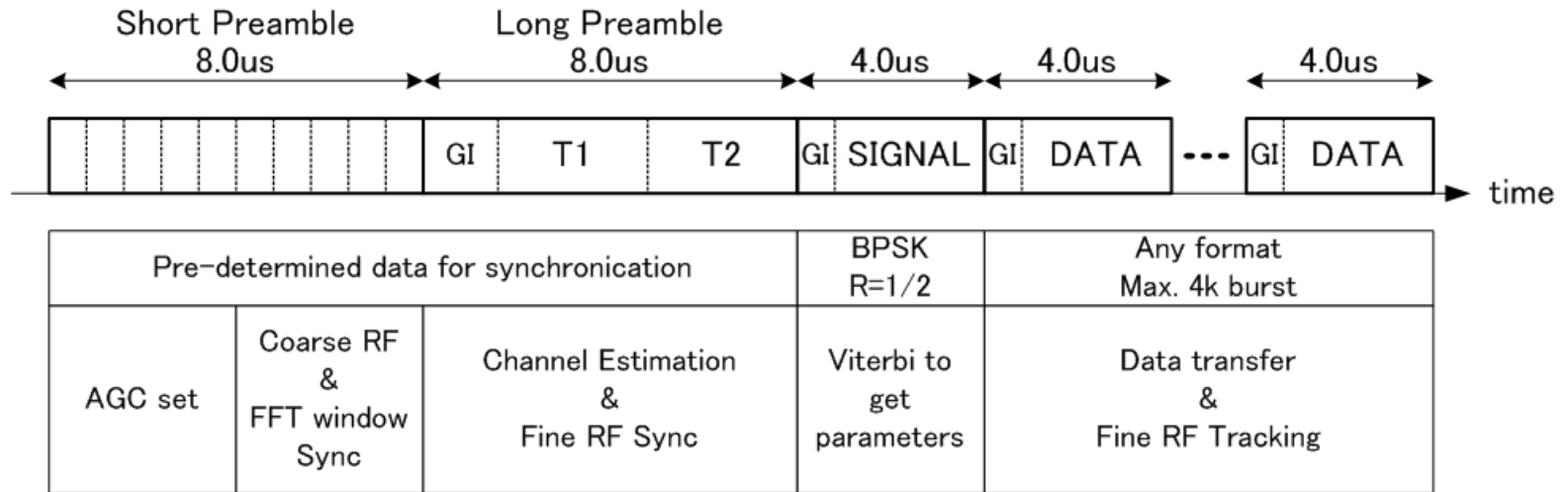


# OFDM WLAN SYSTEM SPEC

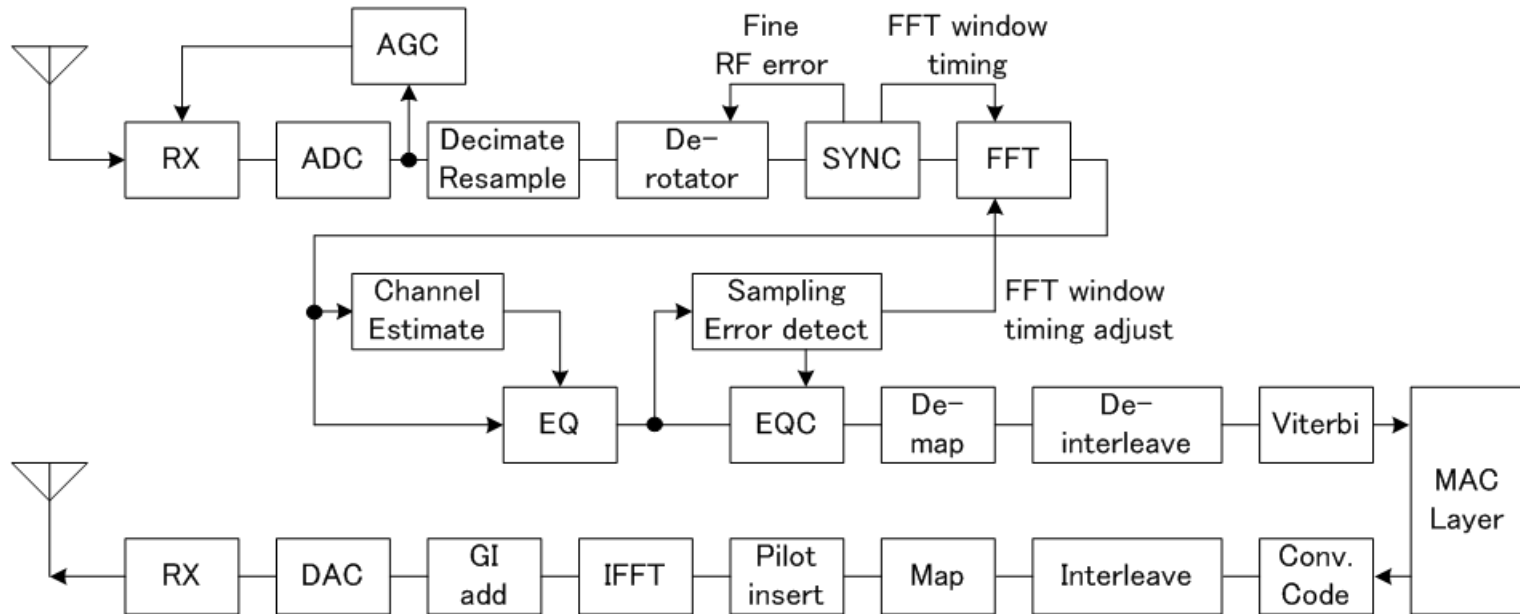
- **802.11a: 5GHz BAND**
- **802.11g: 2.4GHz BAND**

Data rate (Mbps)	6	9	12	18	24	36	48	54
Modulation	BPSK	BPSK	QPSK	QPSK	16QAM	16QAM	64QAM	64QAM
Code rate	1/2	3/4	1/2	3/4	1/2	3/4	2/3	3/4
# of subcarriers	52							
# of pilots	4							
OFDM symbol length	4us (effective symbol=3.2us)							
Guard Interval length	0.8us							
Subcarrier spacing	312.5kHz = 1/3.2us							
Sampling rate	20MHz (50ns)							

# WLAN frame format and receiver tasks



# WLAN Block Diagram





# **EXAMPLE 2)**

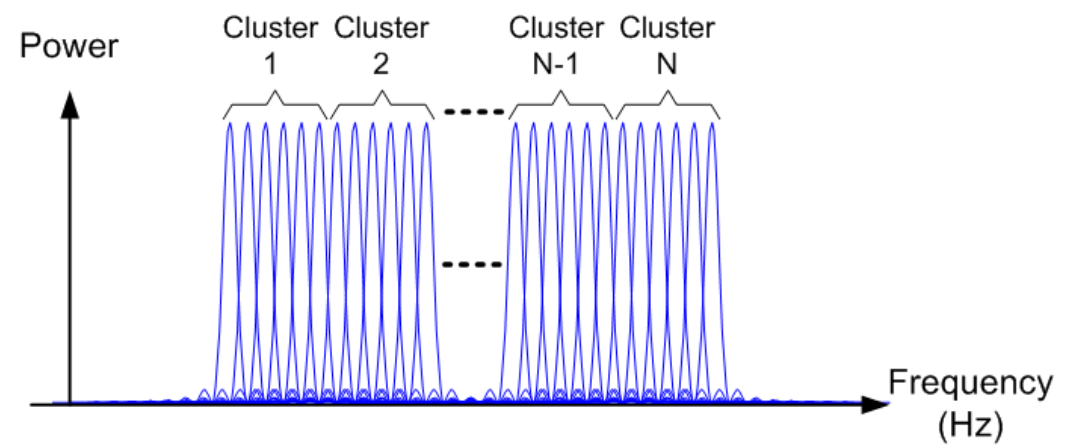
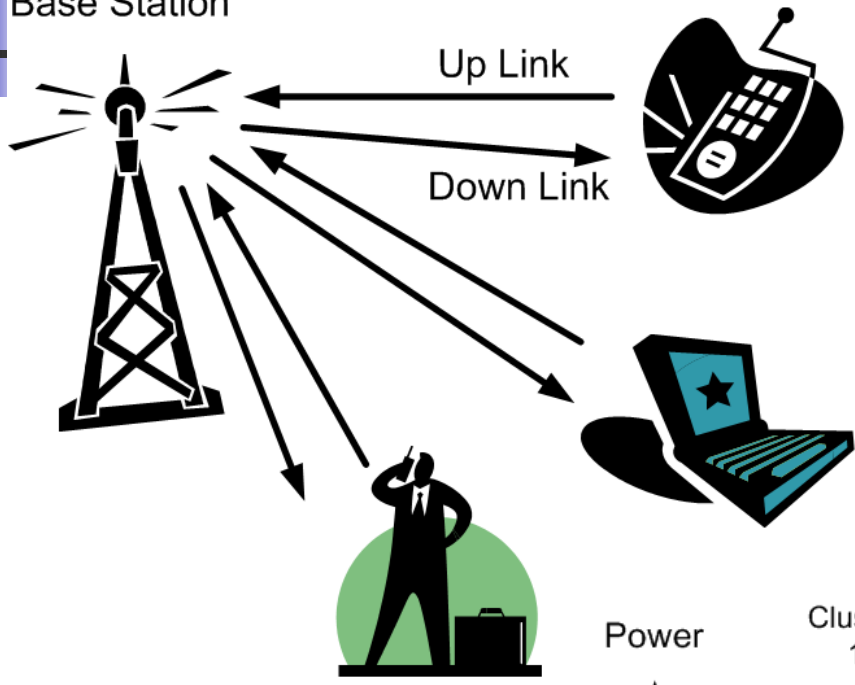
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**LTE**

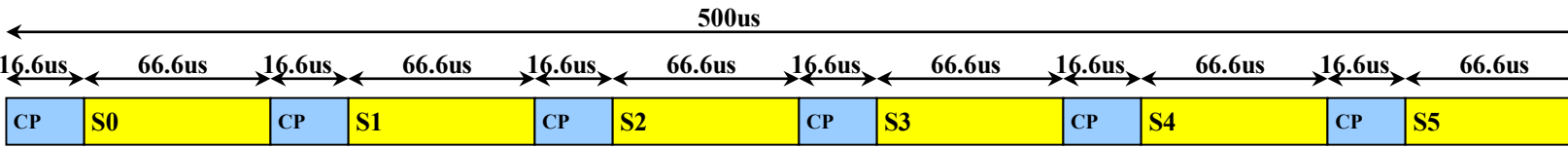
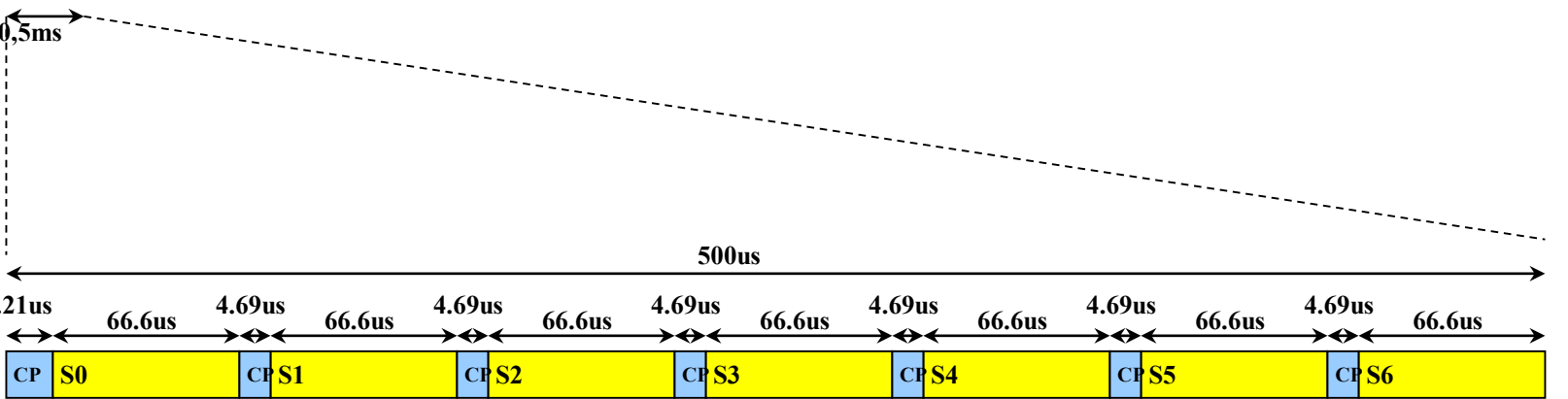
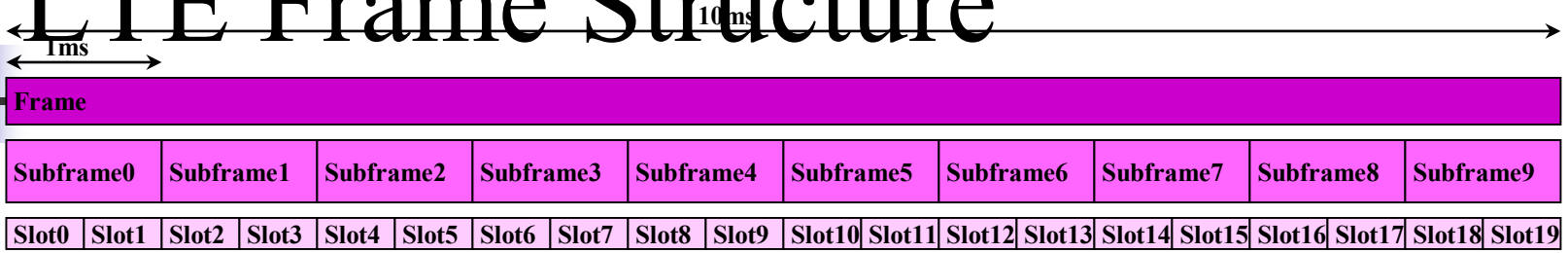
**Long Term Evolution**

# LTE is OFDMA transceiver

Base Station



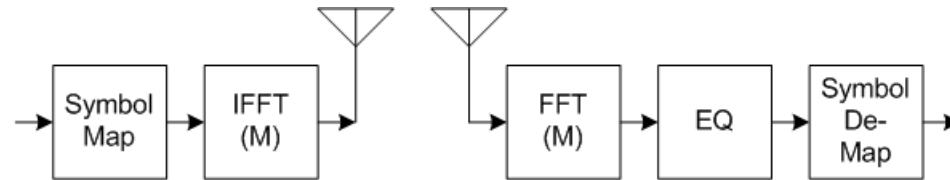
# LTE Frame Structure



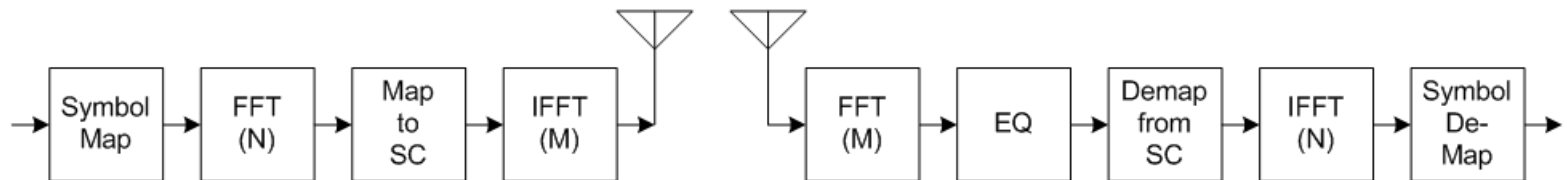


# OFDMA and SC-FDMA

- **Down Link is OFDMA**
- **Up Link us SC-FDMA**

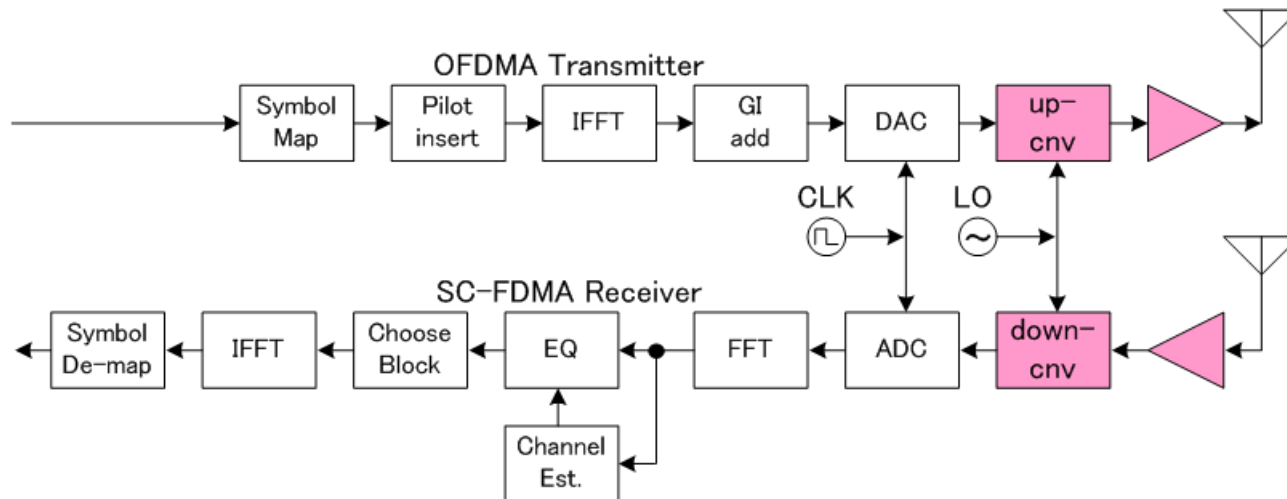


(a) OFDMA

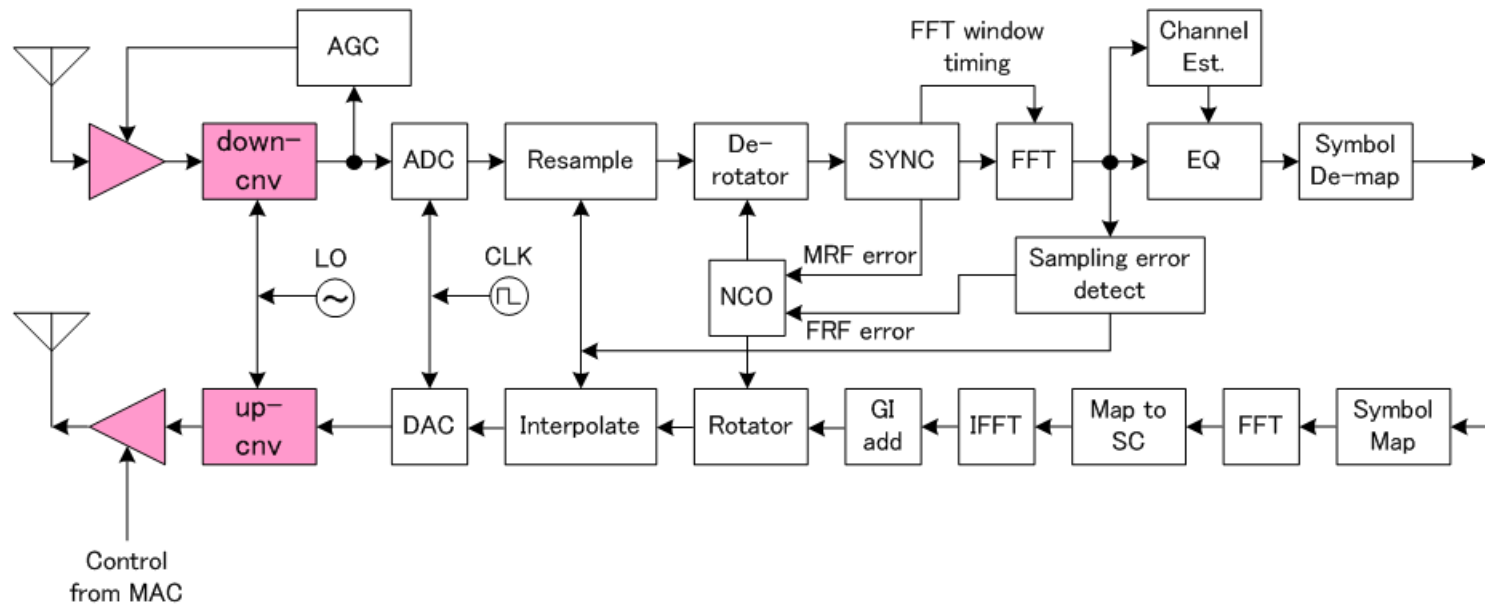


(b) SC-FDMA

# Base Station TX and RX



# User Terminal TX and RX





# Summary

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- High performance Computer and Communication support current IT Society.
- Main stream Technology of High Bandwidth Wireless Communication is based on OFDM method.
- OFDM power spectrum is rectangle then high efficiency is realized.
- WLAN and LTE examples are briefly covered.

# Matlab lab on Dec/14<sup>th</sup> 1:00PM

- Dec/14<sup>th</sup> Saturday, 1pm to 5pm is Matlab lab at computer center, please prepare your login ID

